



EURAMET European Metrology Network for Quantum Technologies: Quantum Metrology and Single Photon Detector calibration

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EMN-Q Chair & INRIM



**QUANTUM
TECHNOLOGIES**

ISSW 2022

The International SPAD Sensor Workshop

Outline



Quantum metrology

- ... as quantum enhanced measurements
- ... according to **metrologists**
- ... for **quantum technologies**

Paradigmatic example:

Single-photon Detectors calibration

A coherent European effort: ***EMN-Quantum***

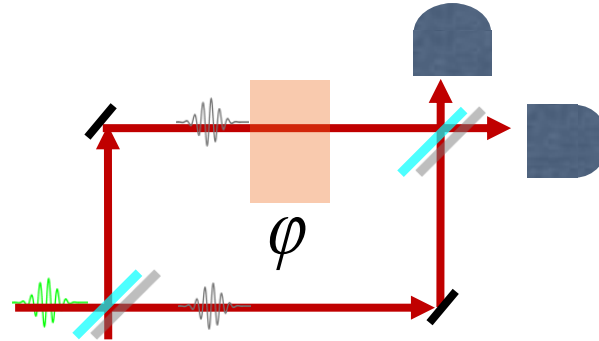


Quantum Enhanced Measurement

Quantum Metrology, Imaging and Sensing with photons

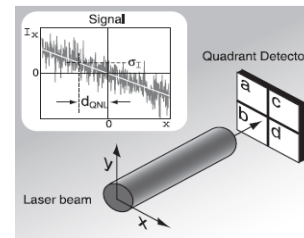
The Shot-Noise Limit

- phase
- Interferometry
- GW detectors



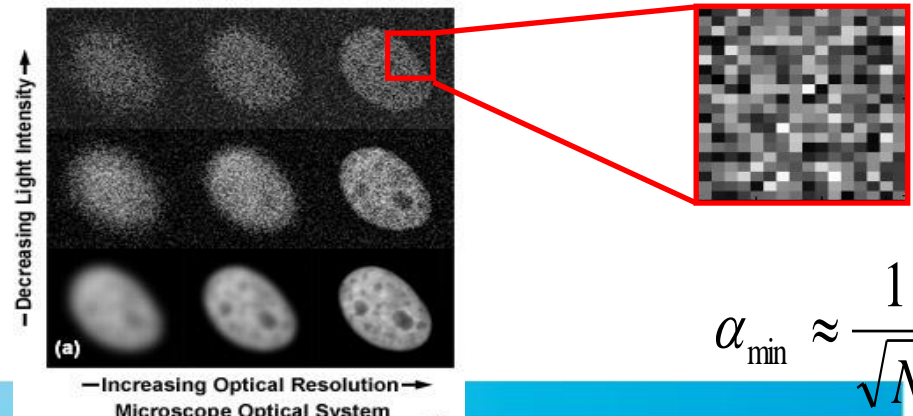
$$\Delta\phi_{\min} \approx \frac{1}{\sqrt{N}}$$

- Displacement:
- lithography
- beams, particles tracking



$$X_R \approx \lambda \frac{f}{D} \quad \Delta x_{\min} \approx \frac{X_R}{\sqrt{N}}$$

- Absorption/reflection:
- Imaging
- microscopy
- Target recognition



$$\alpha_{\min} \approx \frac{1}{\sqrt{N}}$$

Quantum Enhanced Measurement

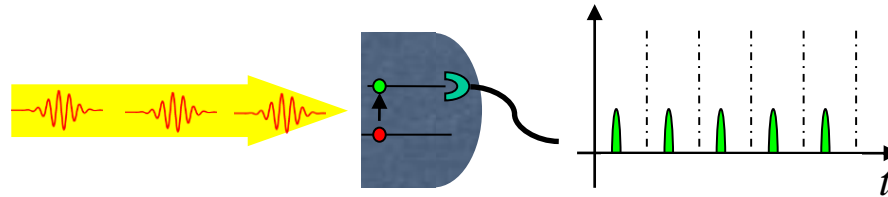
Quantum Metrology, Imaging and Sensing with photons



However quantum mechanics predicts existence of quantum states of light which allow to beat the shot-noise limit

Fock state $|N\rangle$

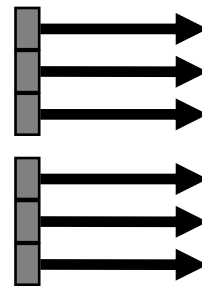
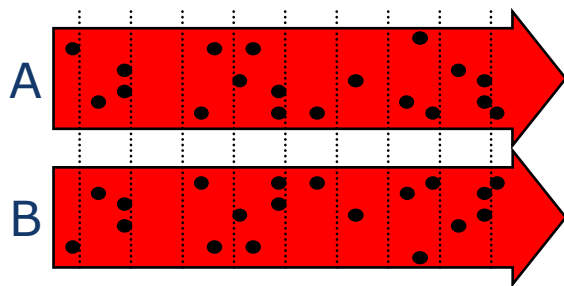
Single photon source : $|1\rangle$



$$\Delta N \approx 0!!!$$

non-classical correlation and entanglement :

Twin beam:
$$|\Psi_{AB}^{(TWB)}\rangle = \prod_{\mathbf{k}} \left[\sum_n C_{\mathbf{k}}(n) |n_{\mathbf{k}}\rangle_A |n_{-\mathbf{k}}\rangle_B \right]$$



$N_1(t)$
 $N_2(t)$
 $N_3(t)$
 $N_3'(t)$
 $N_2'(t)$
 $N_1'(t)$

$$\sigma = \frac{Var(N_i - N'_i)}{\langle N_i + N'_i \rangle} < 1$$



QUANTUM



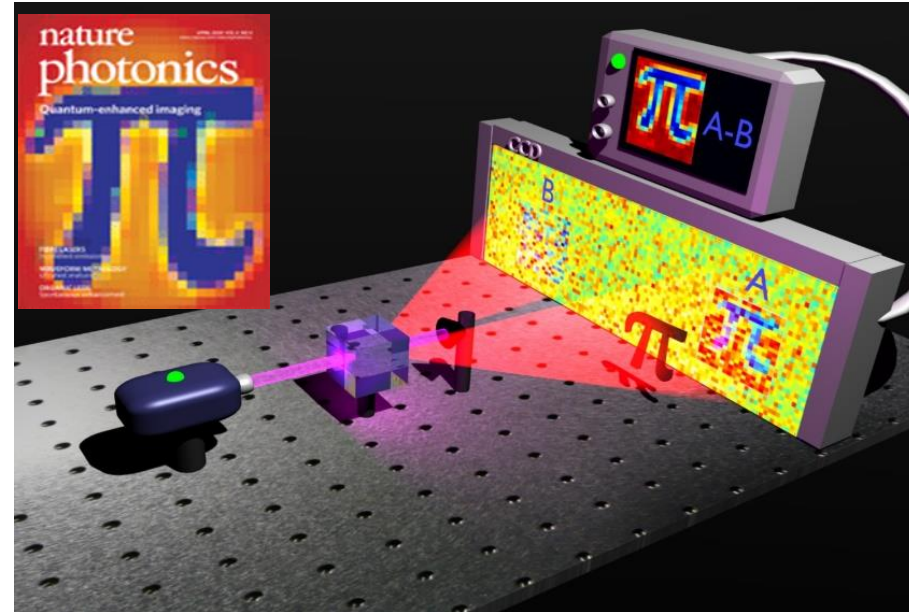
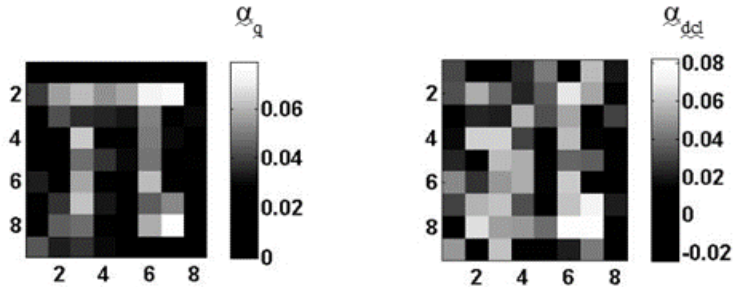
Quantum Enhanced Measurement

Quantum Metrology, Imaging and Sensing with photons

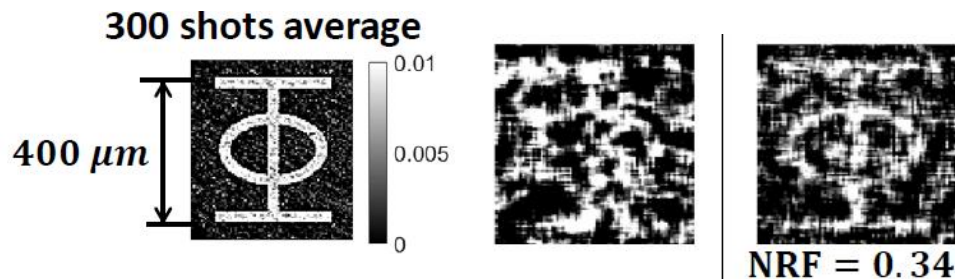


Sub-Shot Noise Imaging

Beating the shot-noise with quantum light



Wide-Field Sub-Shot Noise Microscope



5 μm resolution



Light S&A 6, e17005 (2017)

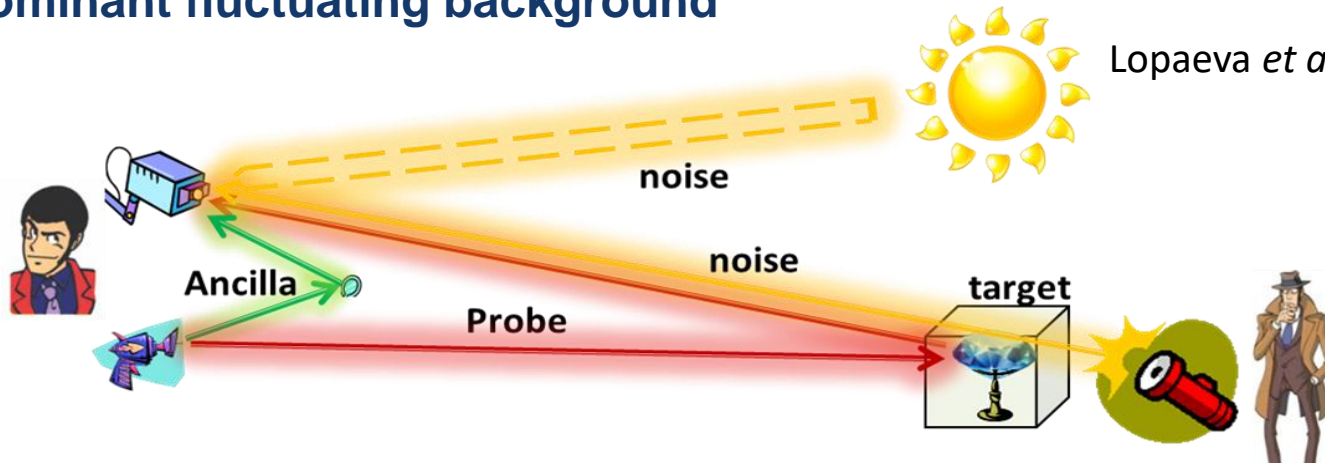
Quantum Enhanced Measurement

Quantum Metrology, Imaging and Sensing with photons



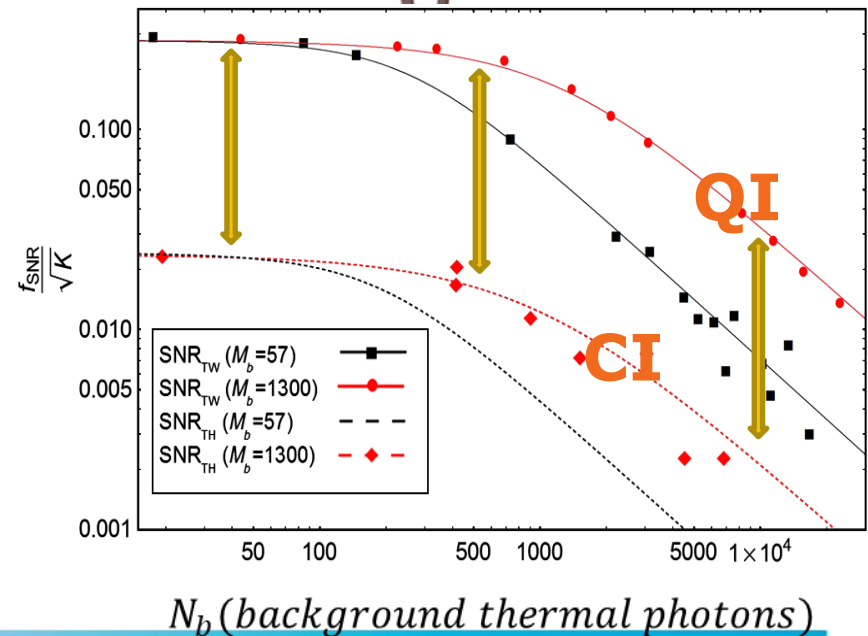
Problem: detection of a partially reflecting target which is immersed in a dominant fluctuating background

Lopaeva *et al*, PRL 110, 153603 (2013)



Quantum illumination takes advantage of an ancillary beam, quantum correlated /entangled with the probe, by a joint measurement of the two.

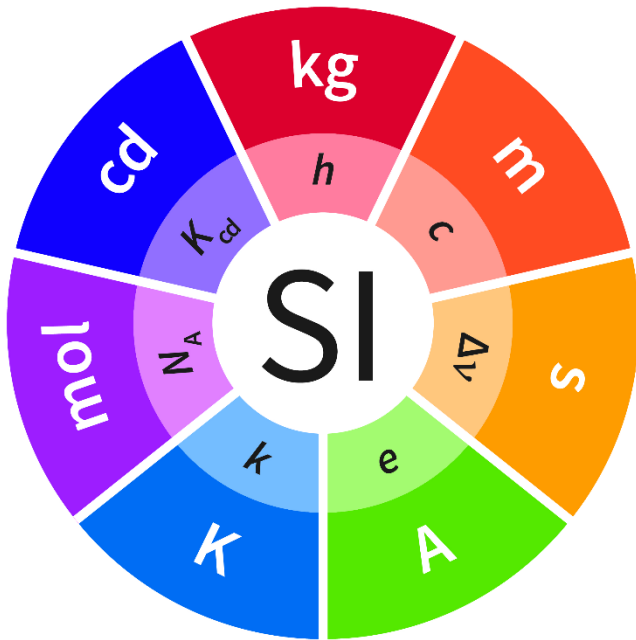
- ✓ **Large quantum enhancement!**
- ✓ **Independent of noise and losses!**
- ✓ **Non-classical signature does not survive the noise**



Quantum Metrology... according to metrologists

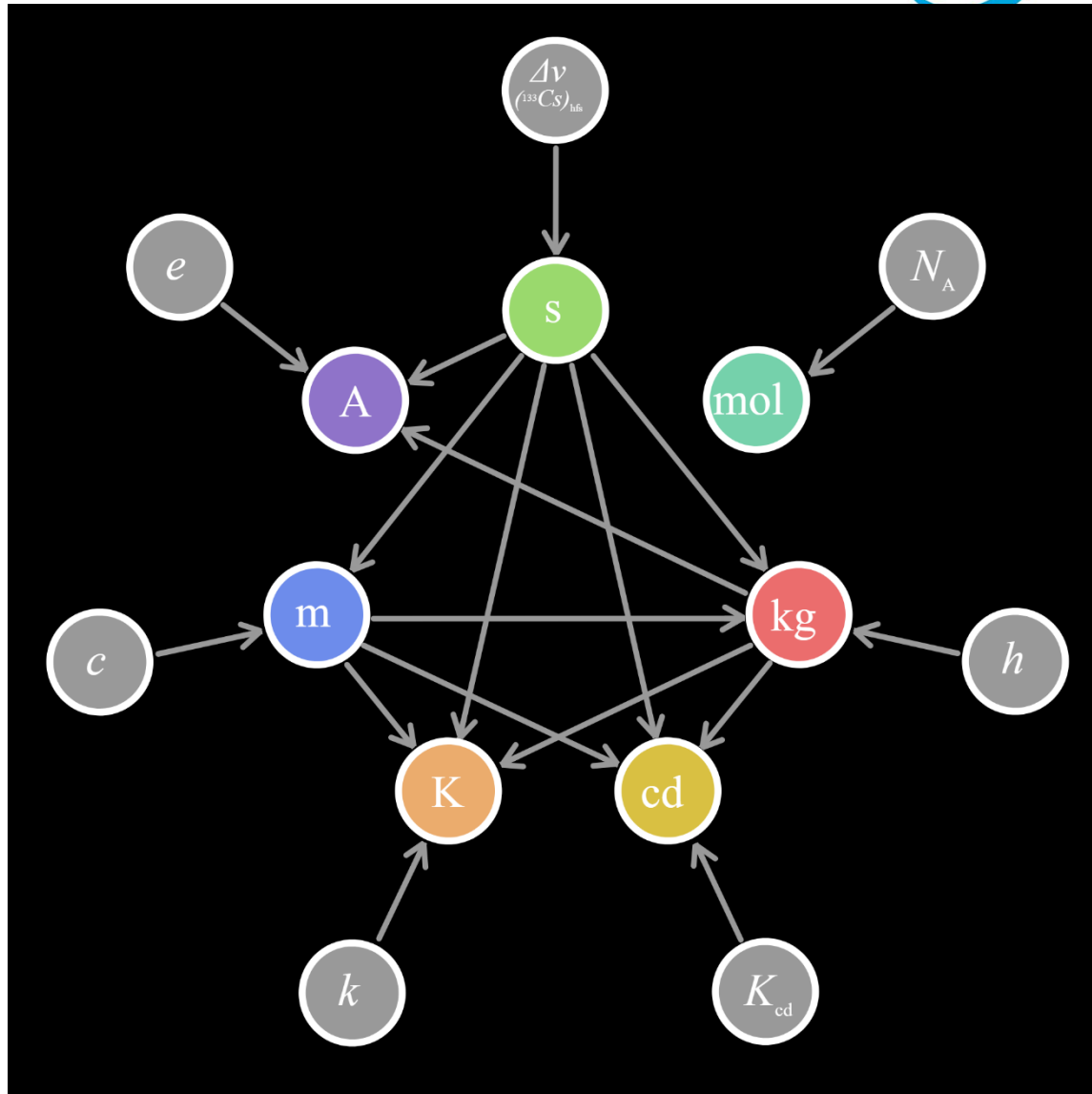


The New SI ...



November 2018

26th General Conference on Weights and Measures (CGPM)



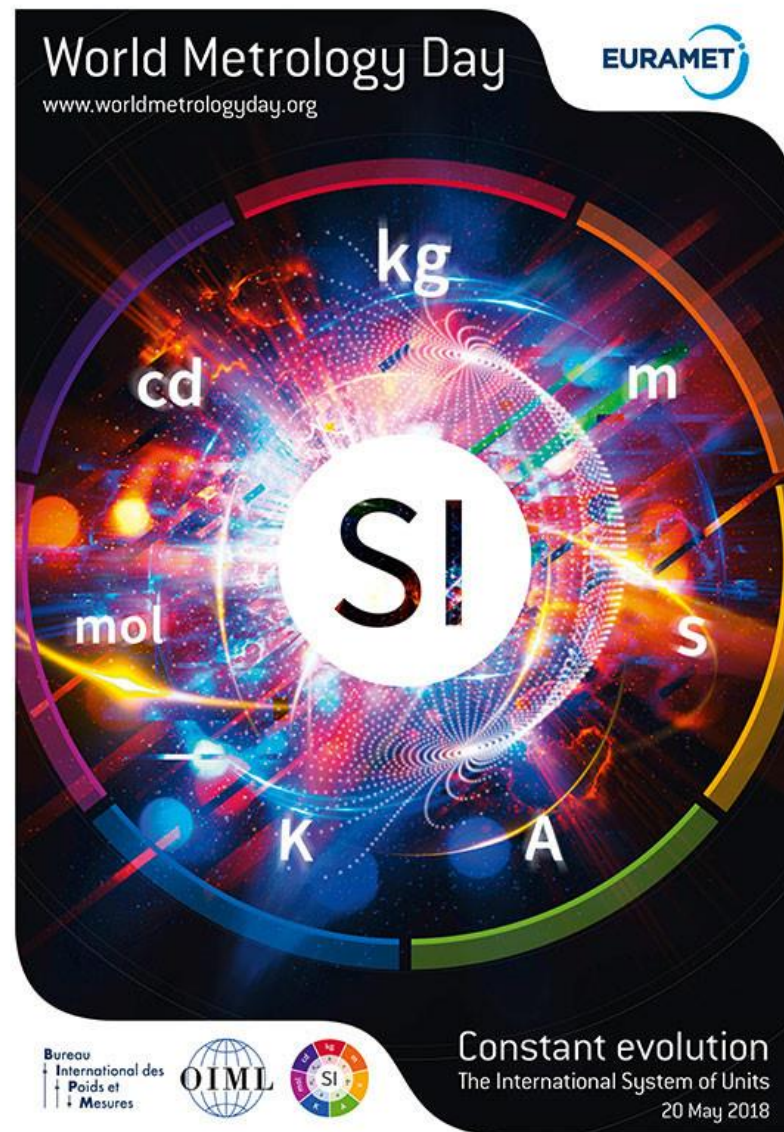
Quantum Metrology... according to metrologists



The **SI** and its defined units are not static.

The progress in science, in particular in the area of laser physics, quantum optics, solid-state physics, and nanotechnology, has now paved the way for an upcoming fundamental **revision of the SI**.

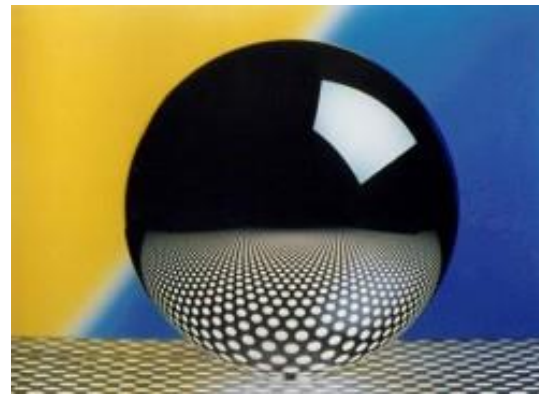
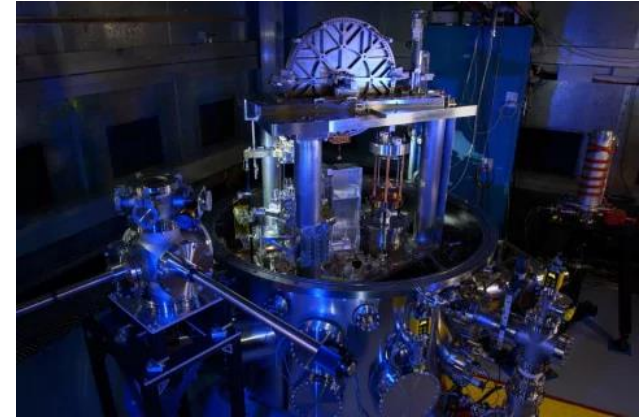
The physics and technology behind the **new SI** definitions and their realization is (mostly) **quantum**.



Quantum Metrology... according to metrologists

The kilogram is defined in terms of the Planck constant

Kibble balance used to calculate Planck's constant.

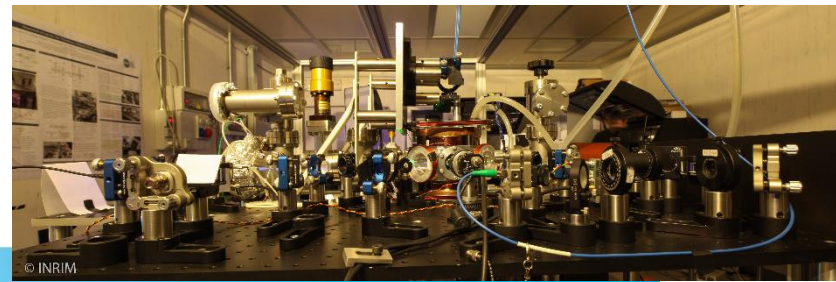


Avogadro sphere (X-ray crystal density) used to estimate the Planck's constant



The second is defined in terms of the hyperfine transition frequency of the caesium 133 atom

Optical Atomic clock

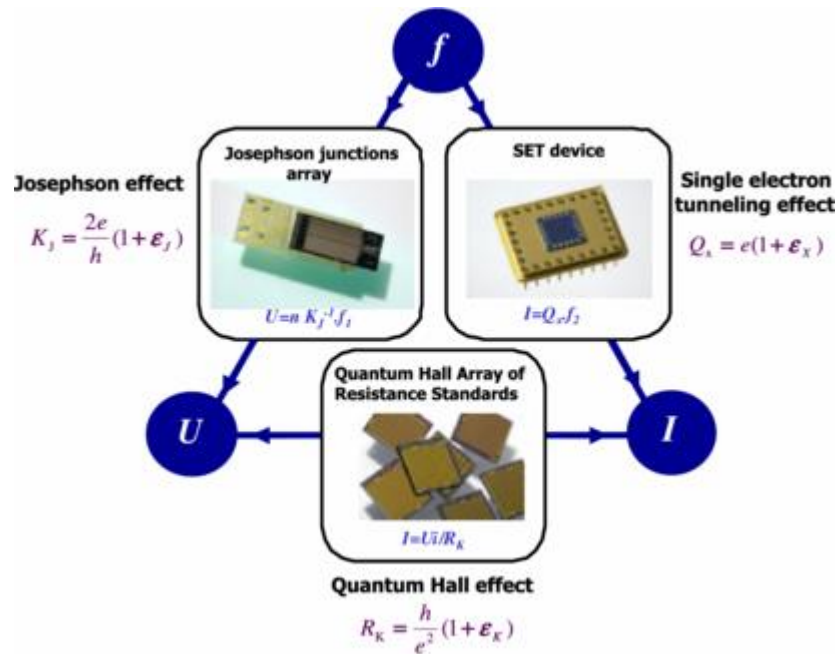


Quantum Metrology... according to metrologists



The Ampere is defined in terms of the electron charge

Quantum metrological triangle: Ohm's law with the three quantum electrical effects: the Josephson effect (JE), the quantum Hall effect (QHE) and the single-electron tunnelling effect (SET)



The Mole is defined in terms of NA

The Kelvin is defined in terms of Boltzmann's constant

The Candela is defined in terms of K_{cd} constant



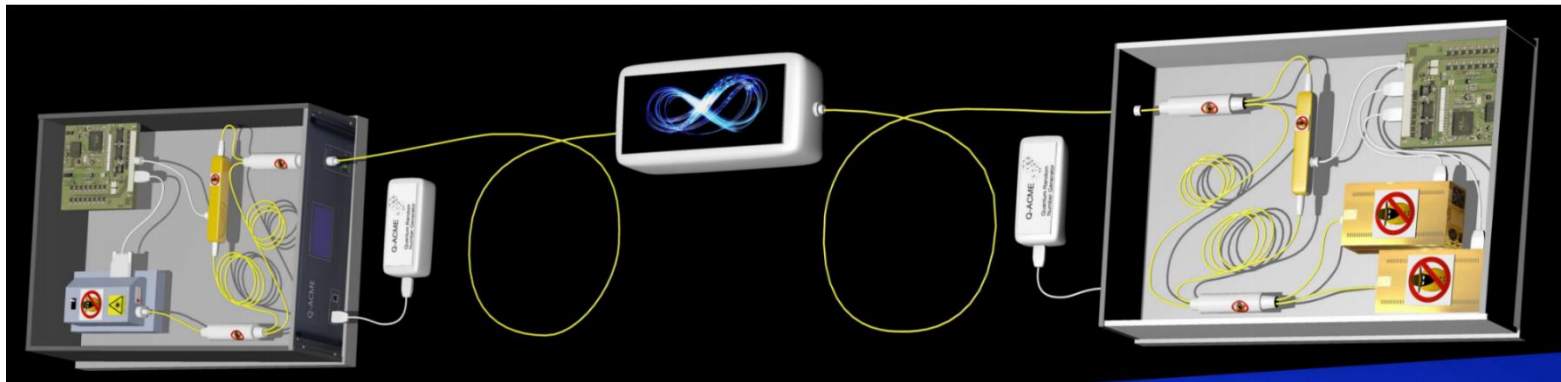
Q-Metrology for Q-Communication



An Industry Specification Group (ISG) of the European Telecommunications Standards Institute (ETSI) has been installed from October 2008 to address **standardization** issues in **QKD**, to support the **commercialization** of QKD devices on various levels and stages.



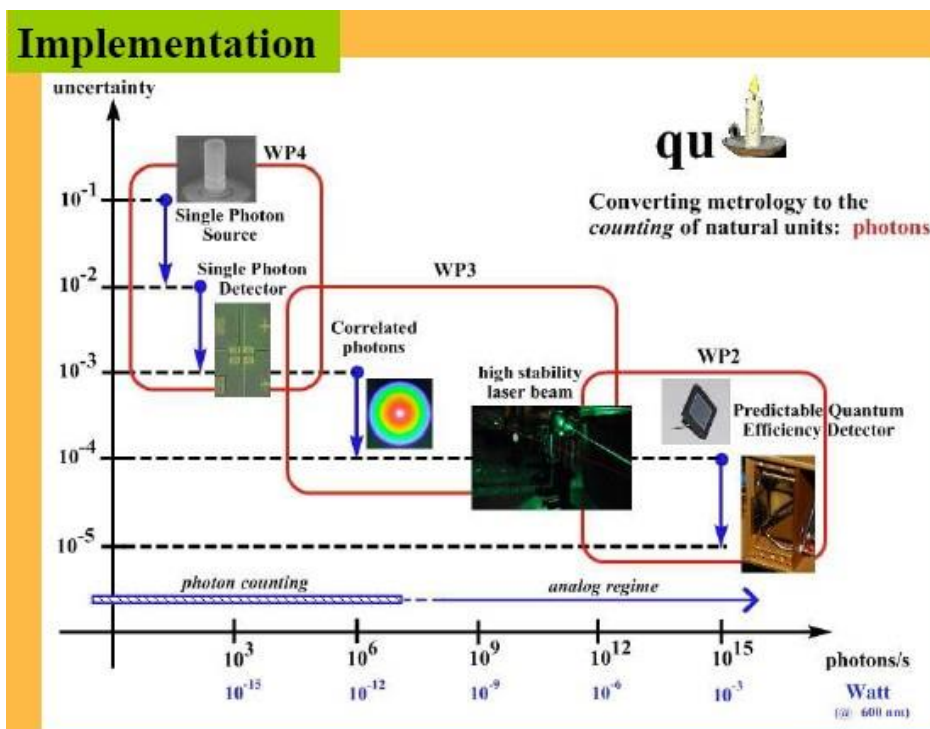
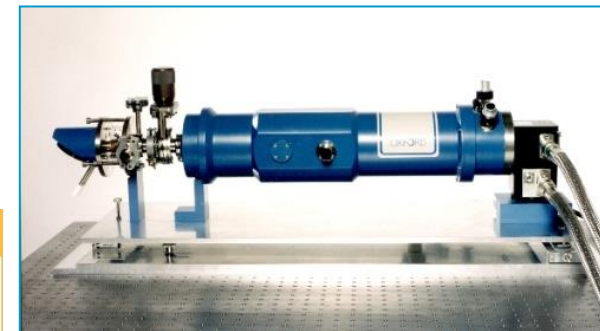
Quantum Radiometry is **necessary** to the standardization framework for providing **traceable** characterization techniques at **single-photon** level.



Q-Metrology for Q-Communication

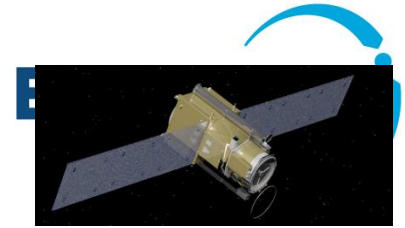


Quantum Radiometry: Effort to create a linkage between the typical optical power measurement regime of conventional radiometry and the single-photon counting regime



Q-Metrology for Q-Communication

Projects on single-photon metrology



Project Coordinator: **INRIM**

Quantum Candela: radiometric measurements in the natural units, the number of photons

EMRP
European Metrology Research Programme
Programme of EURAMET



The EMRP is jointly funded by the EMRP participating countries within EURAMET and the European Union

SIQUTE

Project Coordinator: **PTB**

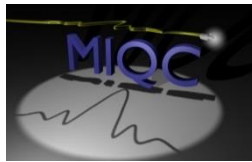
Deterministic and efficient single-photon sources for quantum metrology



EMRP
European Metrology Research Programme
Programme of EURAMET



The EMRP is jointly funded by the EMRP participating countries within EURAMET and the European Union



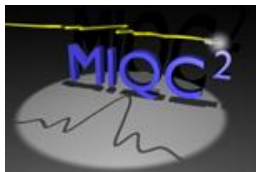
Project Coordinator: **INRIM**

Metrology for Quantum Key Distribution (QKD) in fiber

EMPIR



The EMPIR initiative is co-funded by the European Union's Horizon 2020 research and innovation programme and the EMPIR Participating States



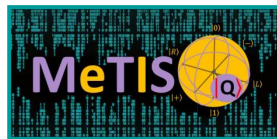
Project Coordinator: **INRIM**

Metrology for free-space QKD and Anti-"Quantum-Hacking"

EMPIR

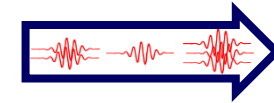


The EMPIR initiative is co-funded by the European Union's Horizon 2020 research and innovation programme and the EMPIR Participating States



Project Coordinator: **INRIM**

Metrology for Testing the Implementation Security of QKD Hardware



EMPIR



The EMPIR initiative is co-funded by the European Union's Horizon 2020 research and innovation programme and the EMPIR Participating States

SIQUEST

Efficient single-photon sources for quantum technologies and quantum metrology

SEQUME

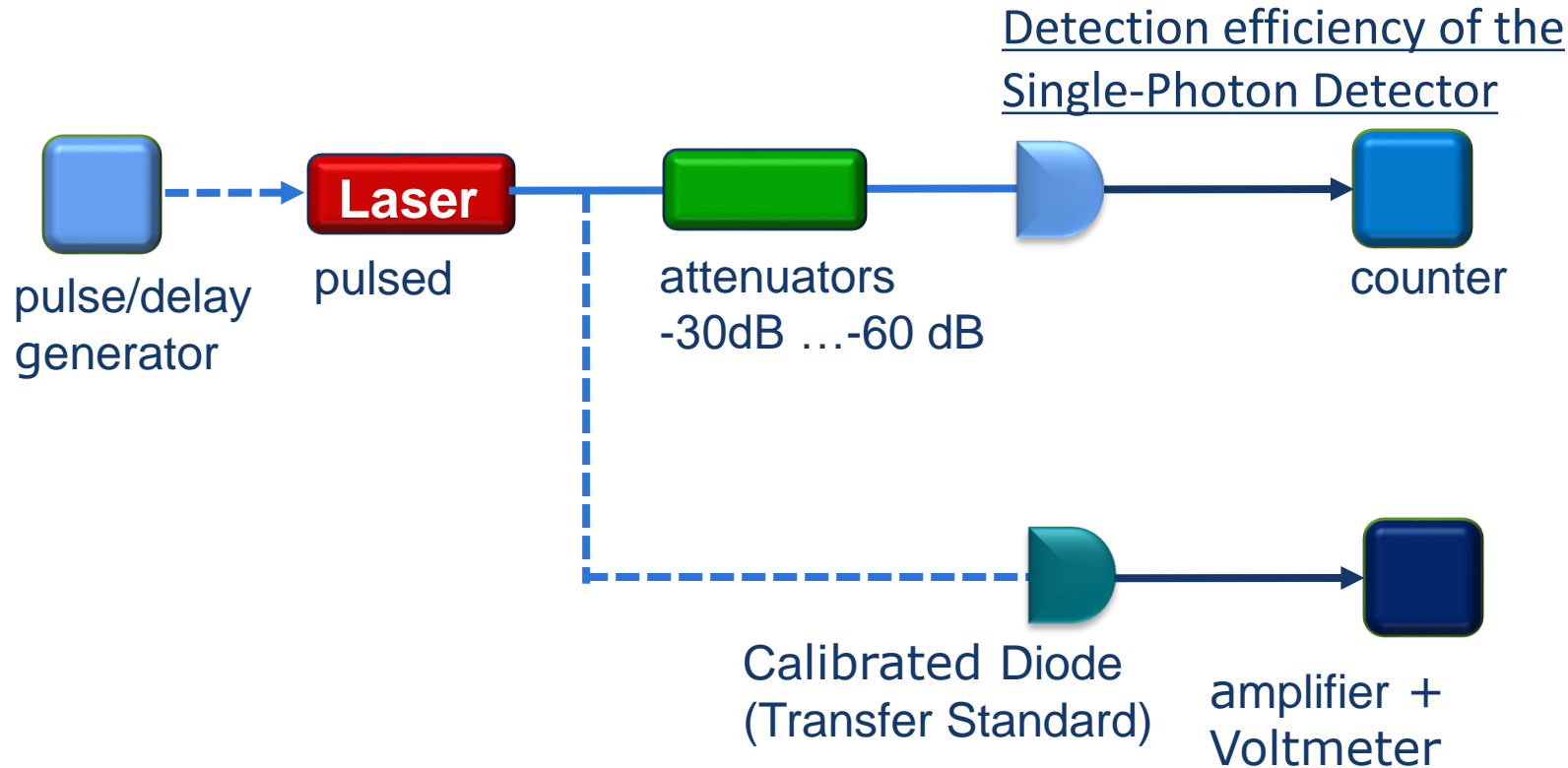
Project Coordinator: **PTB**



QUANTUM TECHNOLOGIES

Detection Probability measurement: Substitution Method

Single-Photon Detection Probability



Issues

- Attenuators Calibration From CW to pulsed source
- Nonlinearity & Deadtimes
- From CW to pulsed source

- ...

Detection Probability measurement: Substitution Method

Optical power traceability chain (SI)

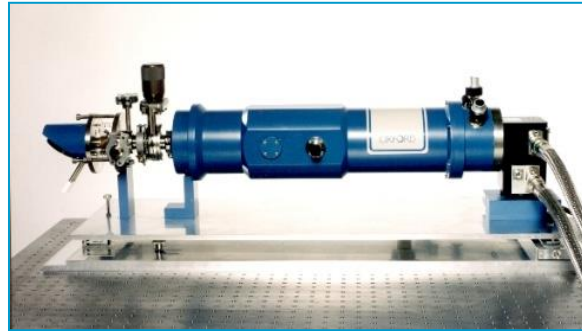
Primary standard
Cryogenic radiometry



NMI reference detectors



Low power
reference
detector



0.005 % uncertainty
visible wavelengths,
0.5 mW,
collimated,
free-space laser radiation

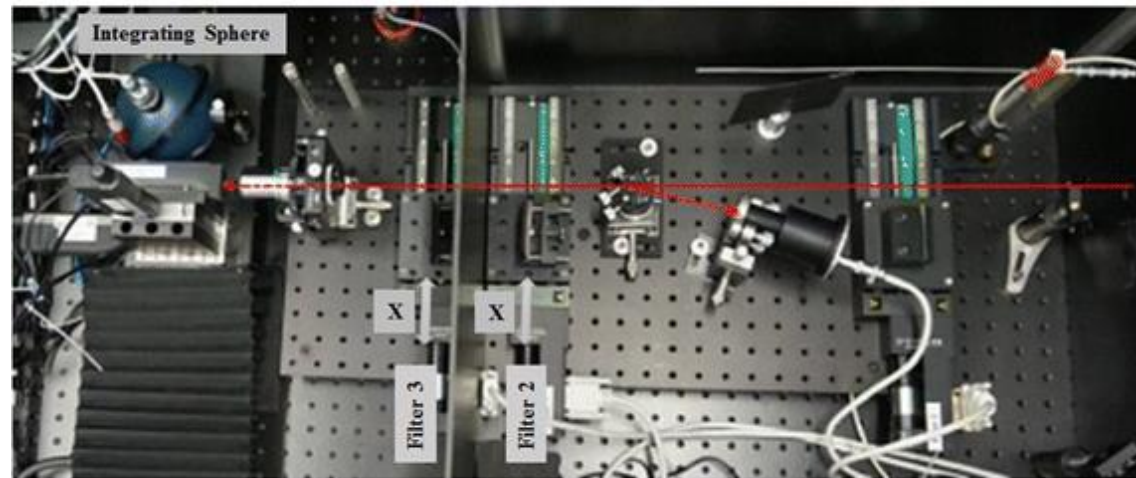
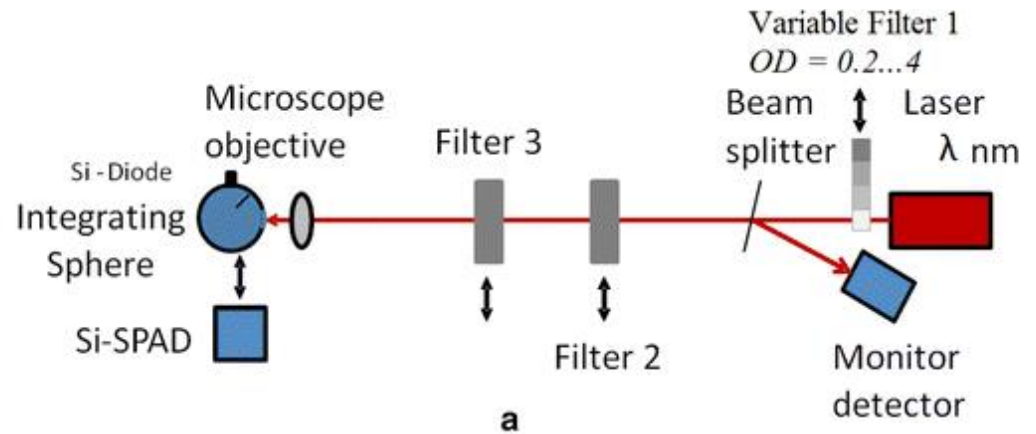


1% uncertainty or less ($k = 2$)
100 pW,
output from optical fibre

Detection Probability measurement: Substitution Method



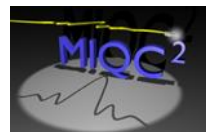
Pilot comparison on the detection efficiency meas. of single-photon detectors @850nm and @1550nm



b

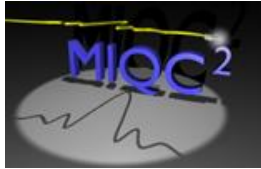
@850 nm
11 NMIs: EU, Asia and America

@1550 nm
Study in MIQC2
4 NMI: INRIM, PTB, NPL and CMI

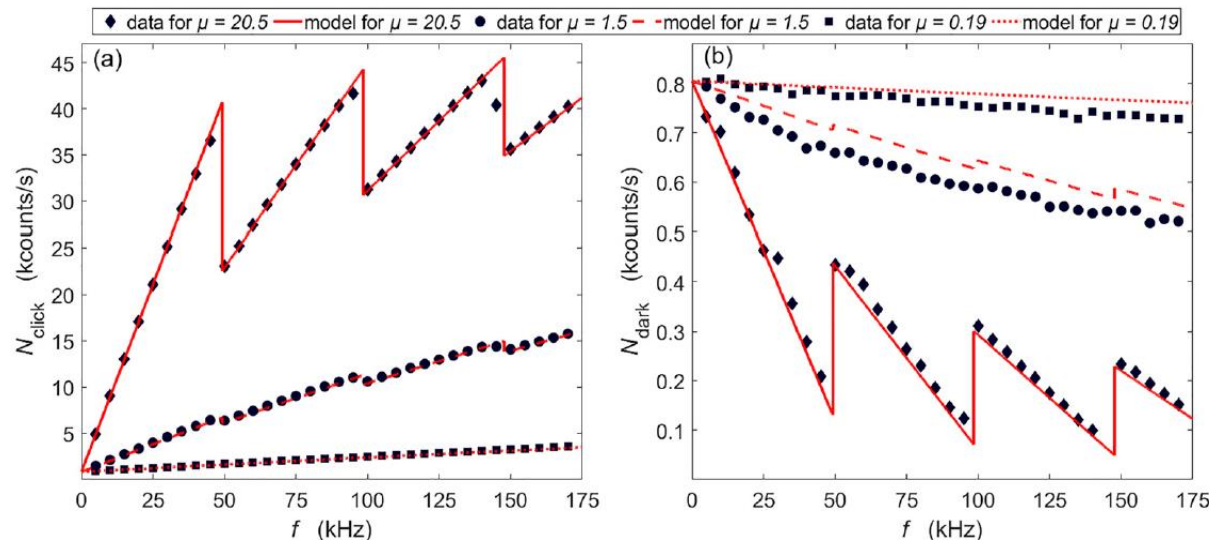
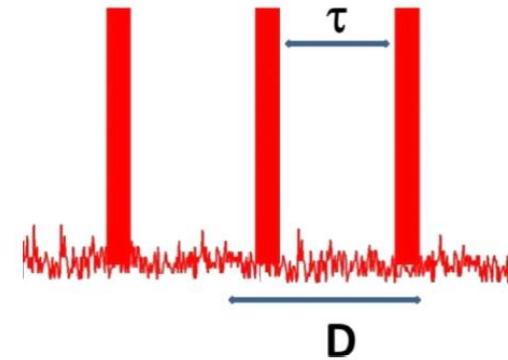
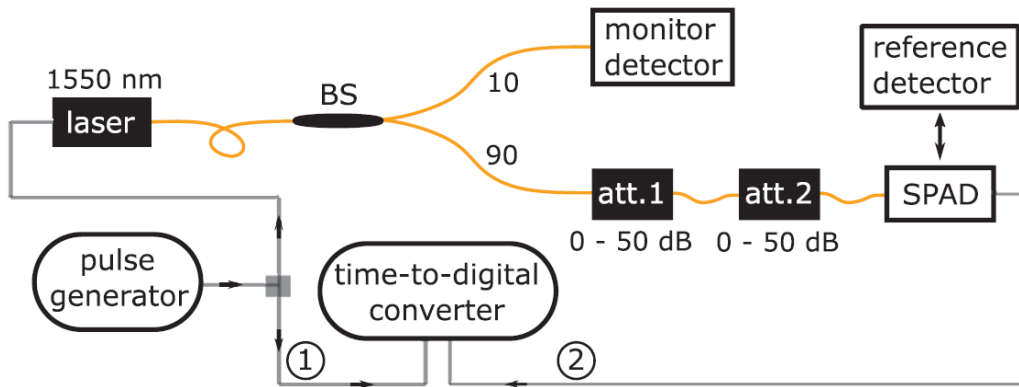


EPJ-QT 7, 14 (2020)
APL 118, 174002 (2021)

Detection Probability measurement: Substitution Method



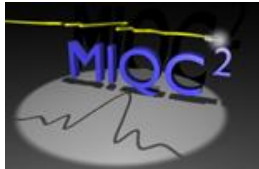
Comparison on the detection efficiency meas. of *free-running* single-photon detectors @1550nm with *pulsed* laser source



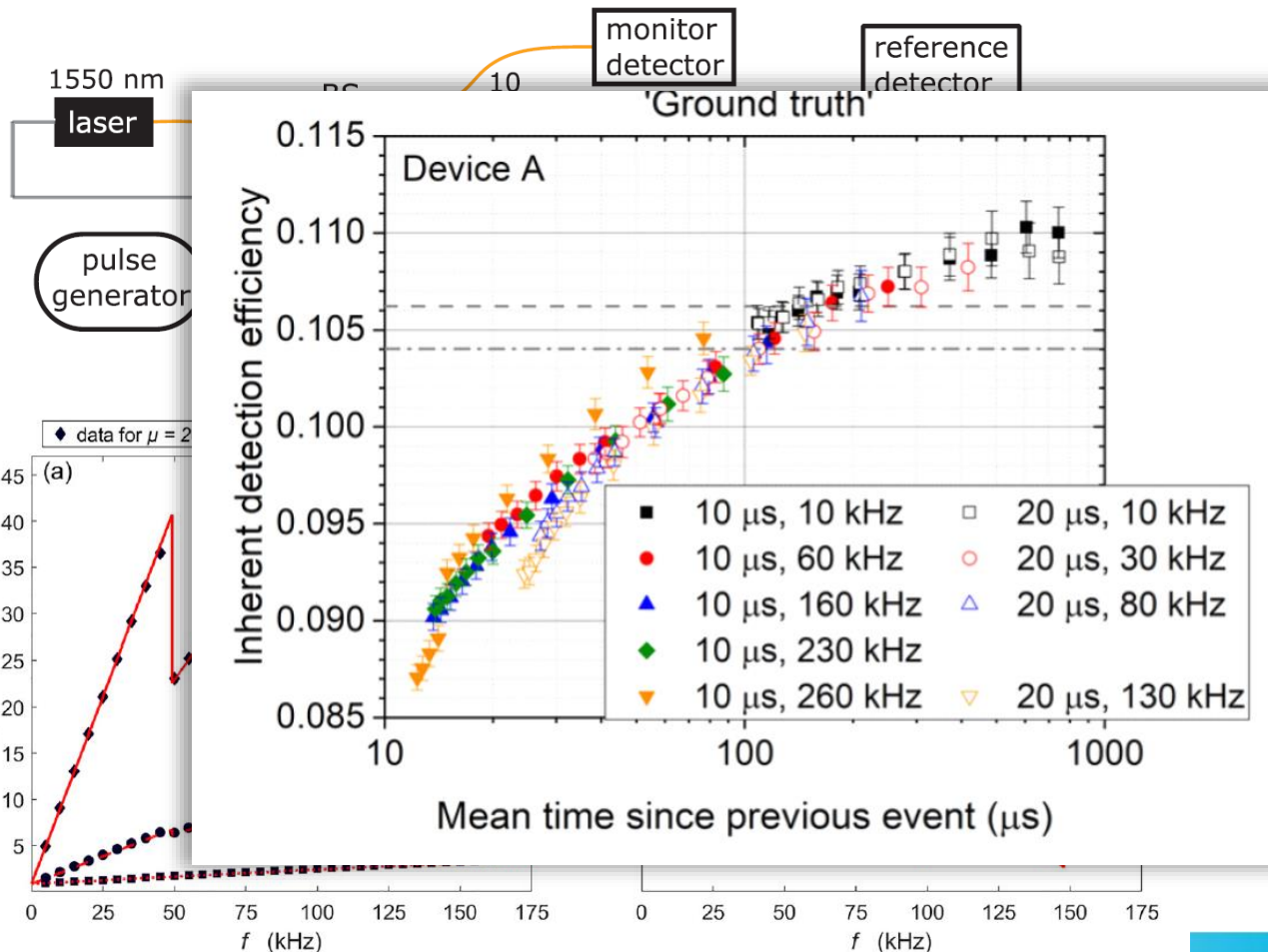
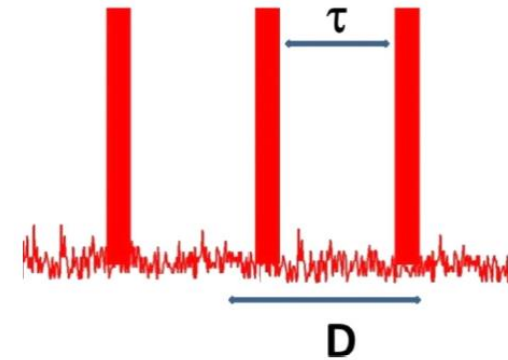
EPJ-QT 7, 14 (2020)
APL 118, 174002 (2021)



Detection Probability measurement: Substitution Method



Comparison on the detection efficiency meas. of *free-running* single-photon detectors @1550nm with *pulsed* laser source

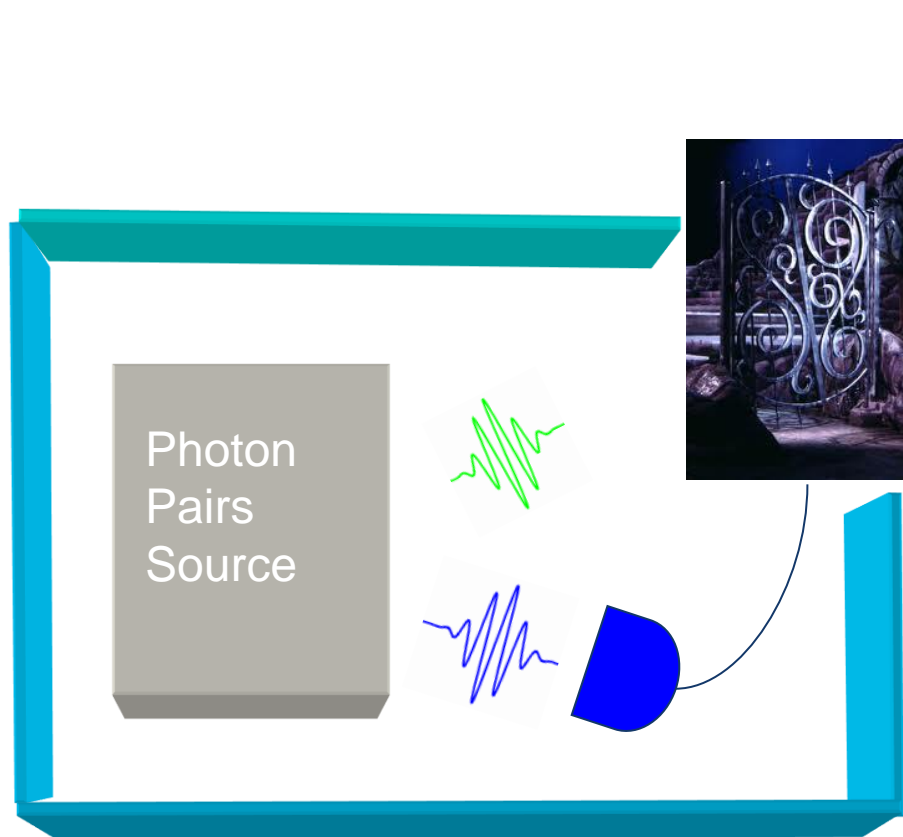


EPJ-QT 7, 14 (2020)
 APL 118, 174002 (2021)
 PRA 105, 042615 (2022)



Detection Probability measurement: Klishko's technique

Detector's quantum efficiency (η) measurement

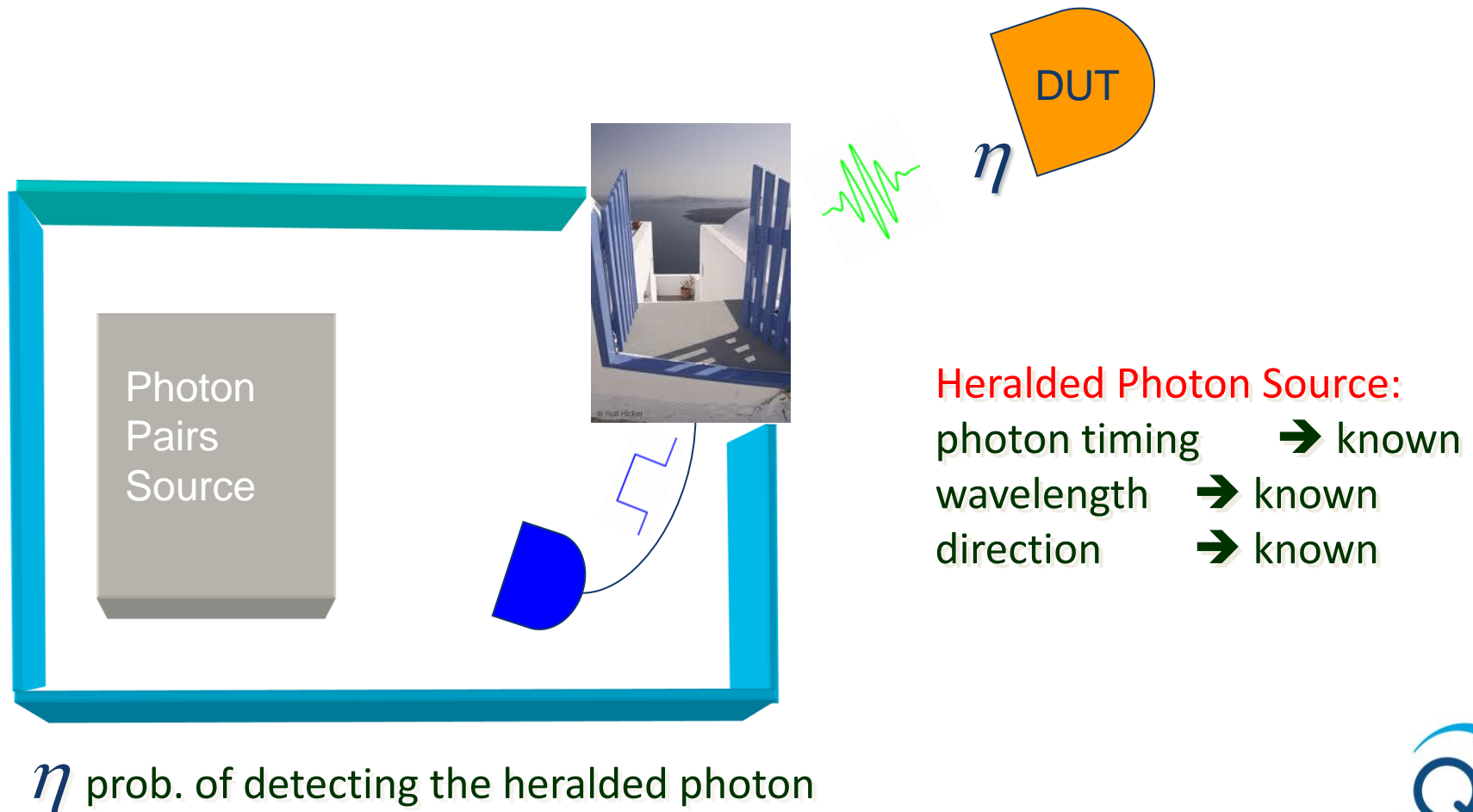


Heralded Photon Source:
photon timing → known
wavelength → known
direction → known

η prob. of detecting the heralded photon

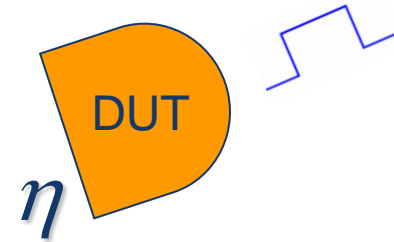
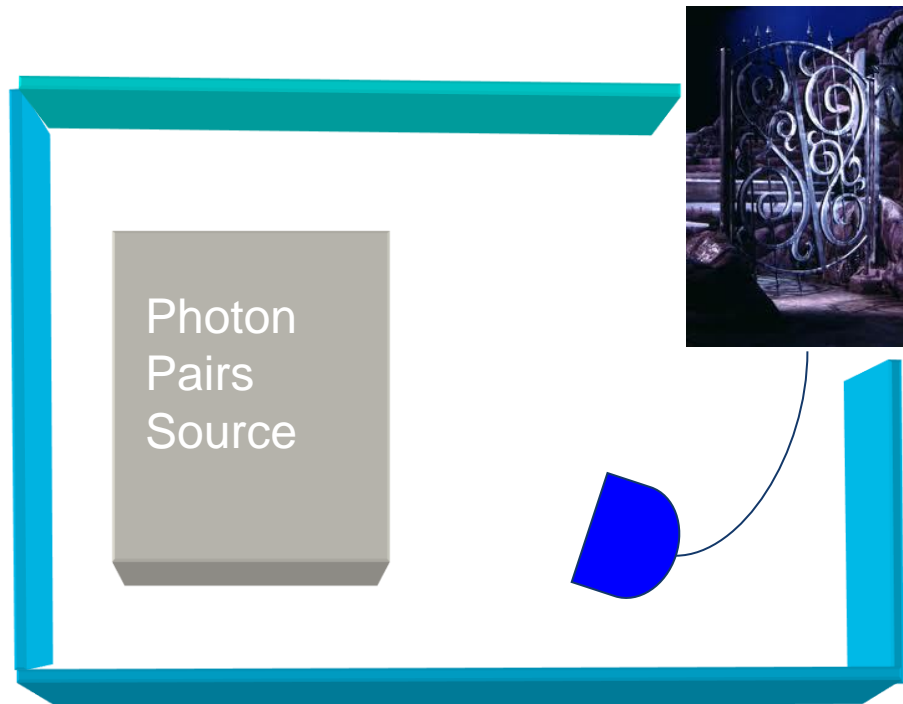
Detection Probability measurement: Klishko's technique

Detector's quantum efficiency (η) measurement



Detection Probability measurement: Klishko's technique

Detector's quantum efficiency (η) measurement



Heralded Photon Source:
photon timing → known
wavelength → known
direction → known

η prob. of detecting the heralded photon

Detection Probability measurement: Klishko's technique

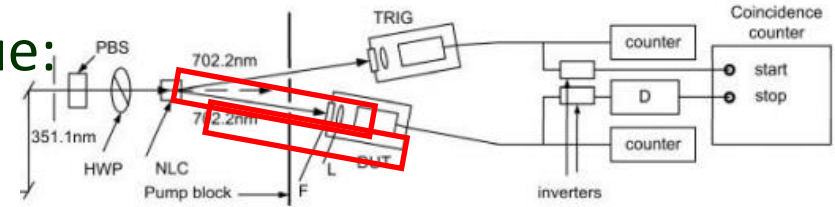


- First experimental implementation (PDC)
[Burnham & Weinberg, PRL **25**, 84 (1970)]

- International research effort:
[Malygin *et al.*, Sov. J. Quantum Electron. **11** 939 (1981); Rarity *et al.*, Appl. Opt. **26**, 4616 (1987); Penin, *et al.*, Appl. Opt. **30** 3582 (1991); Ginzburg *et al.*, Opt. Eng. **32**, 2911 (1993); Kwiat *et al.*, Appl. Opt. **33**, 1844 (1994)...]

- First research effort in the metrological community
[Migdall *et al.*, Metrologia **32**, 479 (1996)]

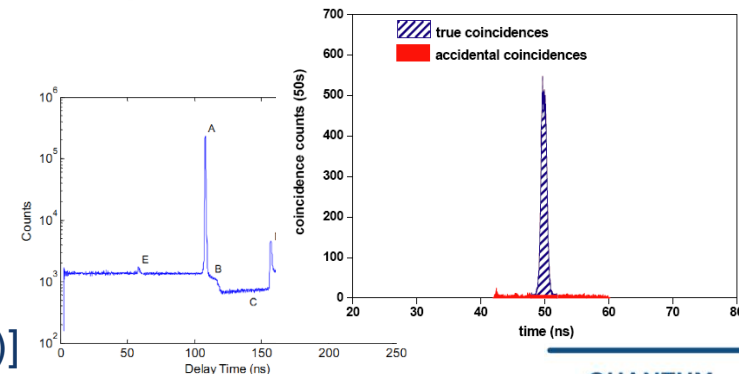
Kt... as a reliable radiometric technique:



Non-idealities to be accounted for

- Optical losses DUT channel
- Accidental coincidences
- Detectors non-linearity, dark counts, after-pulses
- ...

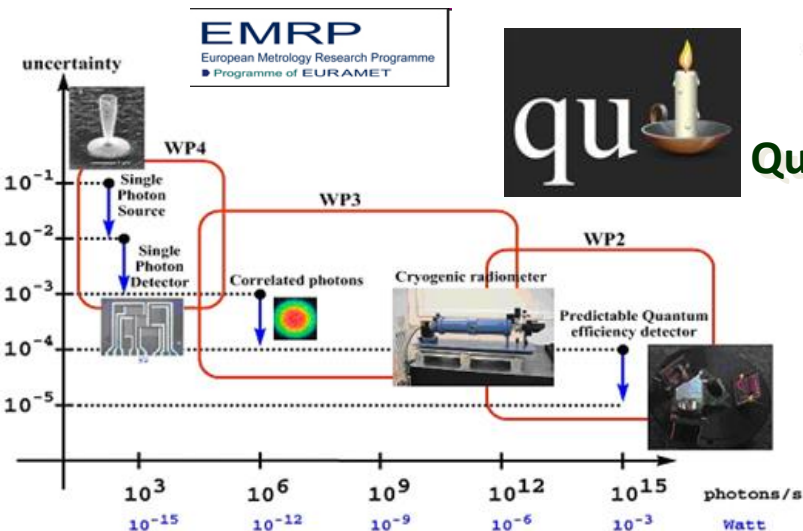
[Polyakov & Migdall, JMO **56**, 1045 (2009)]



Detection Probability measurement: Klishko's technique



... already well established radiometric technique



Lowest relative uncertainties achieved so far: ~0.2%
(comparison with a classical technique traceable to a primary standard)
[Polyakov & Migdall, Optics Express **15**, 1391 (2007)]

Results confirmed by the Qu-Candela consortium
(New low-optical power reference detector)

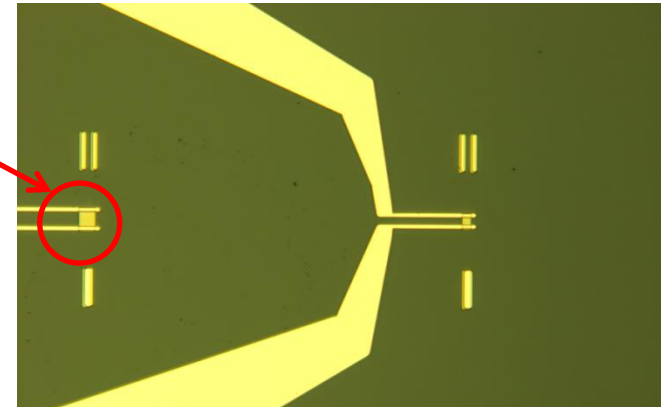
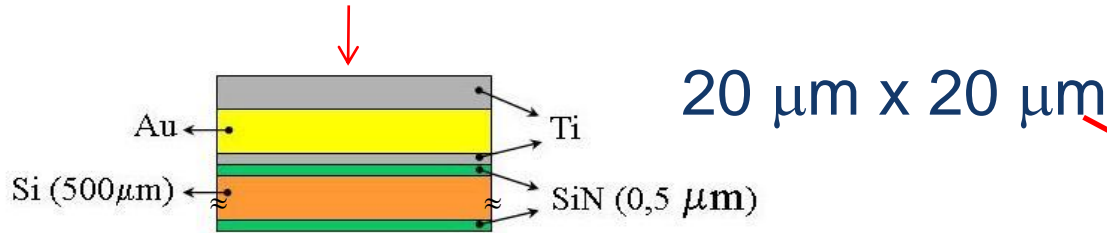
[Cheung et al., Optics Express **19**, 20347 (2011)]



Detection Probability measurement: Klishko's technique: Extension 1



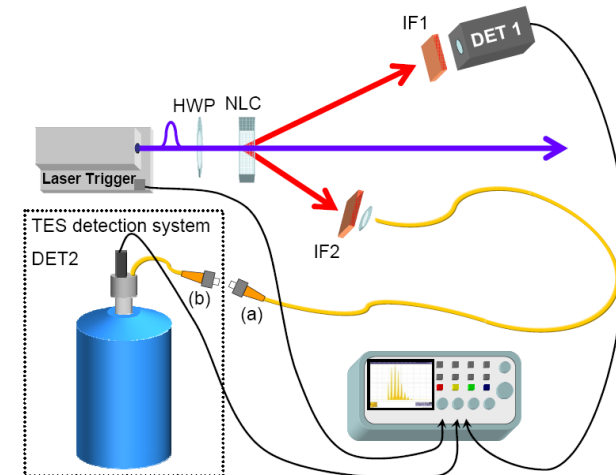
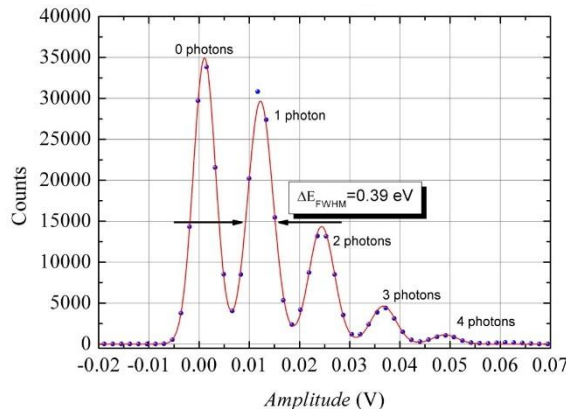
TES - Transition Edge Sensor



TESs are based on a superconducting thin film working as a very sensitive microcalorimeter



PNR detector

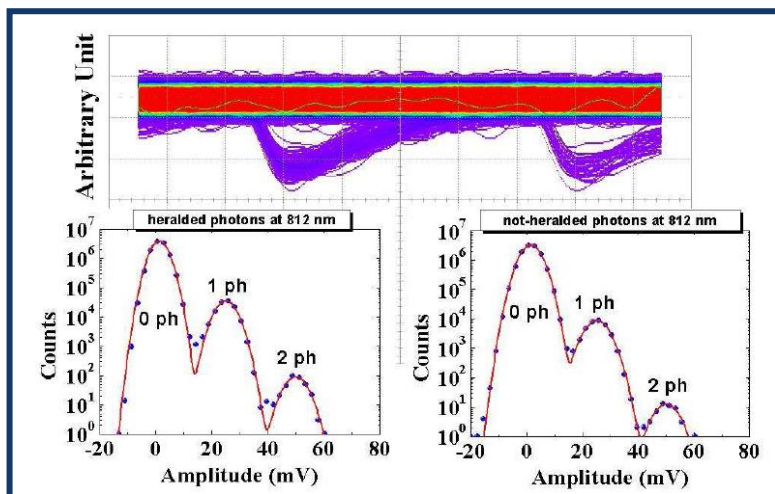


[Optics Express **19**, 23249 (2011)]:

Absolute technique for measuring quantum efficiency:

- based on an **heralded single photon source**
- exploiting the **PNR** ability of the detector

Detection Probability measurement: Klishko's technique: Extension 1



$P(i)$ ($\mathcal{P}(i)$) Probability of observing i photons per heralding count **in the presence/absence** of the heralded photon (i.e. of observing $(i-1)/i$ “accidental” counts)

From **each** $P(i)$ a value of “Total” Quantum Efficiency can be estimated (*Consistency Test*)

From the prob. of 0 :

$$\gamma_0 = \frac{P(0) - \mathcal{P}(0)}{\xi \mathcal{P}(0)}$$

From the prob. of i :

$$\gamma_i = \frac{P(i) - \mathcal{P}(i)}{\xi (\mathcal{P}(i-1) - \mathcal{P}(i))}$$

Detection Probability measurement: Klishko's technique: Extension 2

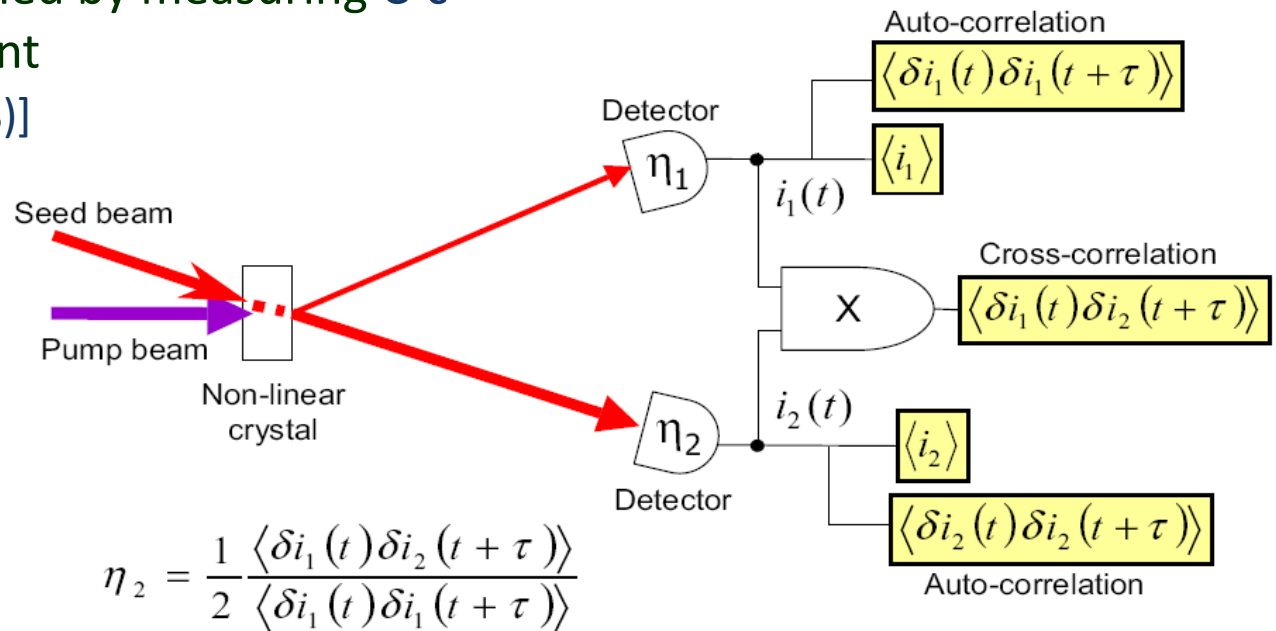
Extension of the KT to the calibration of analog (i.e. not operating at single photon level) detector exploiting twin beam (only in low gain regime)

[JOSAB **23**, 2185 (2006)]

Solution: Seeded Twin Beam

Quantum efficiency obtained by measuring C-c
and A-c of the photocurrent

[Optics Expr. **16**, 12551 (2008)]



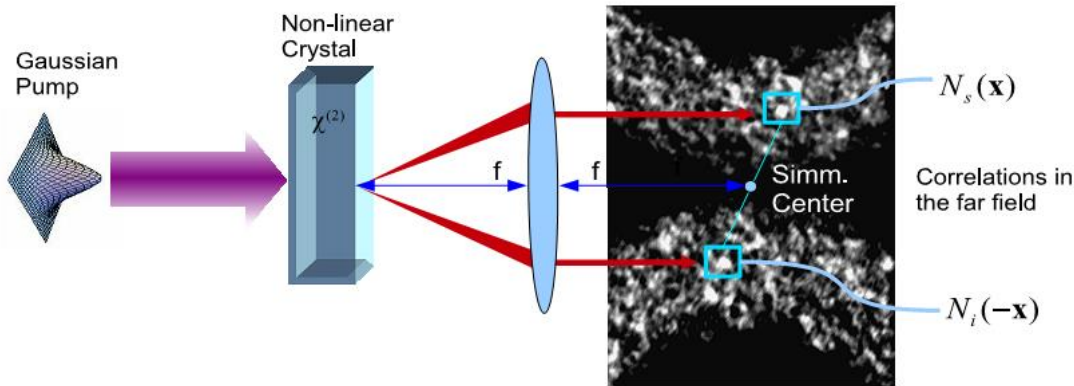
Implementation exploiting a 4 WM in Rb hot vapor

[Marino & Lett, JMO **56**, 401 (2009)]

Detection Probability measurement: Klishko's technique: Extension 3

[Optics Expr. **18**, 20572 (2010); APL **105**, 10113 (2014); Opt. Lett. **41**, 1841 (2016)]

Bright Multimode Twin-Beams used to calibrate scientific CCD camera

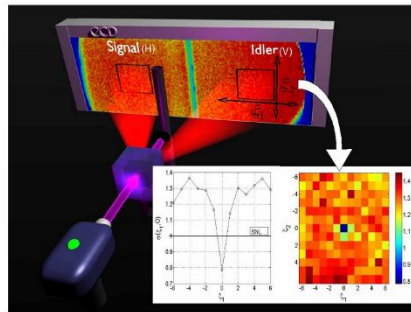


$$|\psi(\mathbf{q})\rangle = \sum_n C_{\mathbf{q}}(n) |n\rangle_{i,\mathbf{q}} |n\rangle_{s,-\mathbf{q}}$$

$$\text{NRF: } \sigma \equiv \frac{\langle \delta^2 N_- \rangle}{\langle N_i + N_s \rangle}$$

$$\langle \delta^2 N_- \rangle \equiv \langle \delta^2 N_s \rangle + \langle \delta^2 N_i \rangle - 2 \langle \delta N_i \delta N_s \rangle$$

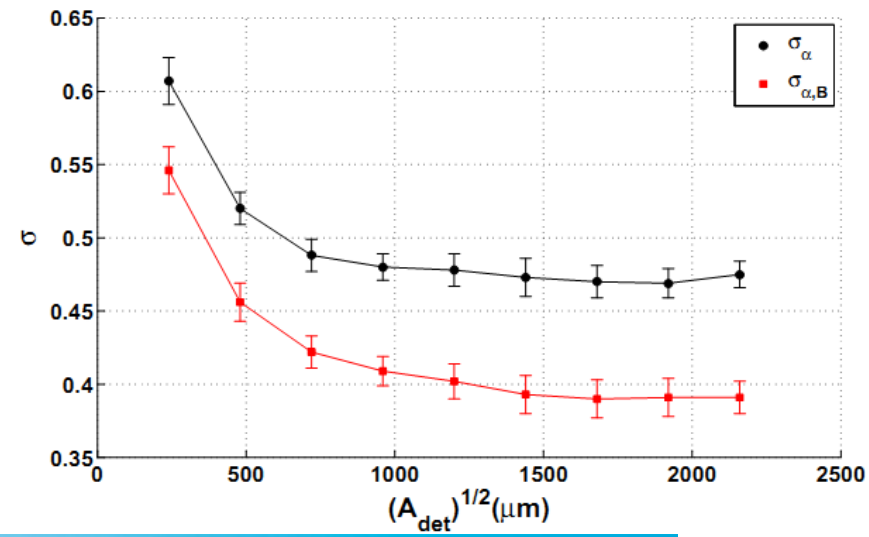
(Sub-Shot Noise Imaging [Nat.Phot.(2010)**4**,227], Quantum Illumination [PRL(2013)**110**,153603])



Corrected NRF

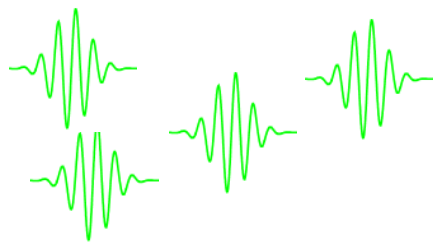
$$\sigma_{\alpha} \equiv \frac{\langle \delta^2 (N_s - \alpha N_i) \rangle}{2 \langle N_s \rangle} = \frac{1}{2} (1 + \alpha) - \eta_s$$

$$\alpha = \langle N_s \rangle / \langle N_i \rangle$$



Detector's POVM tomography

POVM Π_n provides the description of the measurement process



Prob. of output “ n ”

$$p_n = \text{Tr} [\rho \Pi_n]$$

Detector's POVM tomography

POVM Π_n provides the description of the measurement process



$$\Pi_n = \sum_m \Pi_{nm} |m\rangle\langle m|$$

"n"

Prob. of output "n"

$$p_n = \text{Tr} [\rho \Pi_n]$$

Detector's POVM tomography

POVM Π_n provides the description of the measurement process



$$\Pi_n = \sum_m \Pi_{nm} |m\rangle\langle m|$$

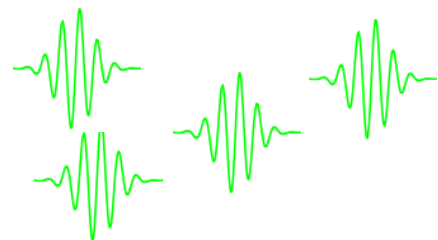
"n"

Prob. of output "n"

$$p_n = \text{Tr} [\rho \Pi_n]$$

Detector's POVM tomography

POVM Π_n provides the description of the measurement process



$$\Pi_n = \sum_m \Pi_{nm} |m\rangle\langle m|$$

"n"

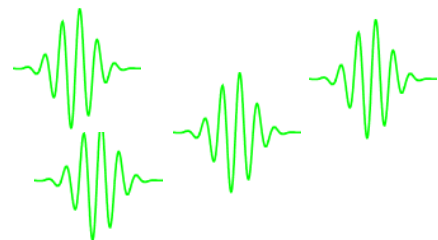
Prob. of output "n"

$$p_n = \text{Tr} [\rho \Pi_n]$$

Π_{nm} : Prob. of having output "n" with m photons as input

Detector's POVM tomography

POVM Π_n provides the description of the measurement process



$$\Pi_n = \sum_m \Pi_{nm} |m\rangle\langle m|$$

“ n ”

Prob. of output “ n ”

$$p_n = \text{Tr} [\rho \Pi_n]$$

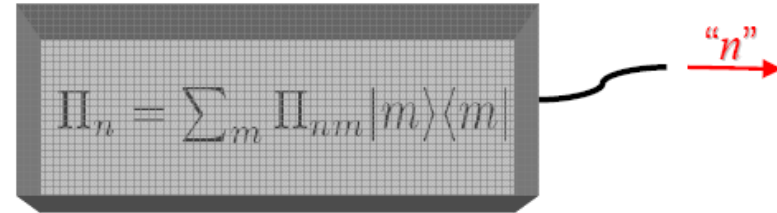
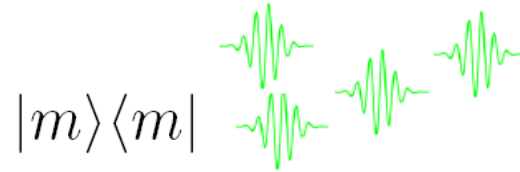
Π_{nm} : Prob. of having output “ n ” with m photons as input

- Quorum of states
- Ancilla assisted

Detector's POVM tomography

Simplest Solution:

Fock state source

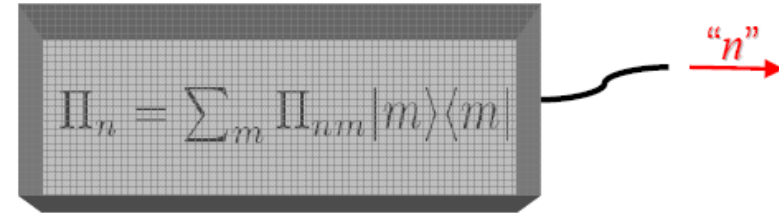
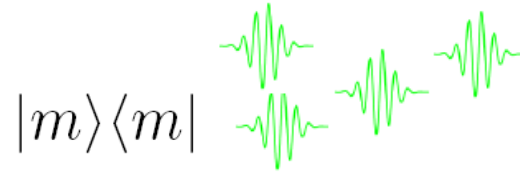


$$p_n = \langle m | \Pi_n | m \rangle = \Pi_{nm}$$

Detector's POVM tomography

Simplest Solution:

Fock state source

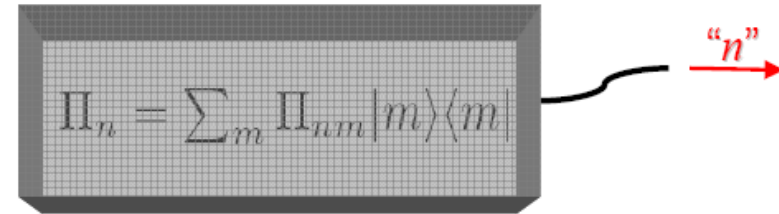
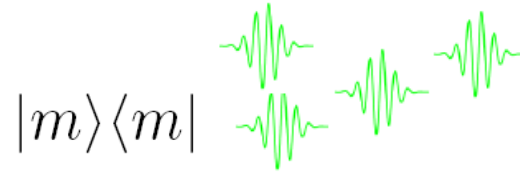


$$p_n = \langle m | \Pi_n | m \rangle = \Pi_{nm}$$

Detector's POVM tomography

Simplest Solution:

Fock state source



$$p_n = \langle m | \Pi_n | m \rangle = \Pi_{nm}$$

Affordable Solution: Coherent source

[Lundeen et al., Nat. Phys 5, 27 (2009)]

$$|\alpha_j\rangle, j = 1, \dots, K$$

$$p_{nj} = \text{Tr}[|\alpha_j\rangle\langle\alpha_j| \Pi_n] = \sum_m \Pi_{nm} q_{mj}$$

$$q_{mj} = \exp(-\mu_j) \mu_j^m / m!$$

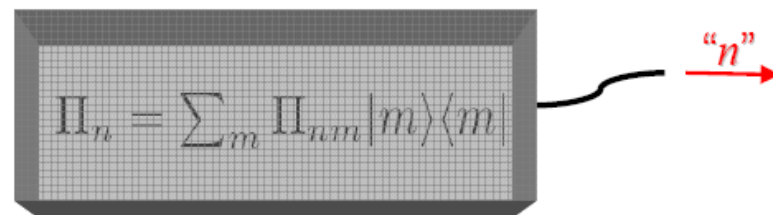
$$\mu_j = |\alpha_j|^2$$



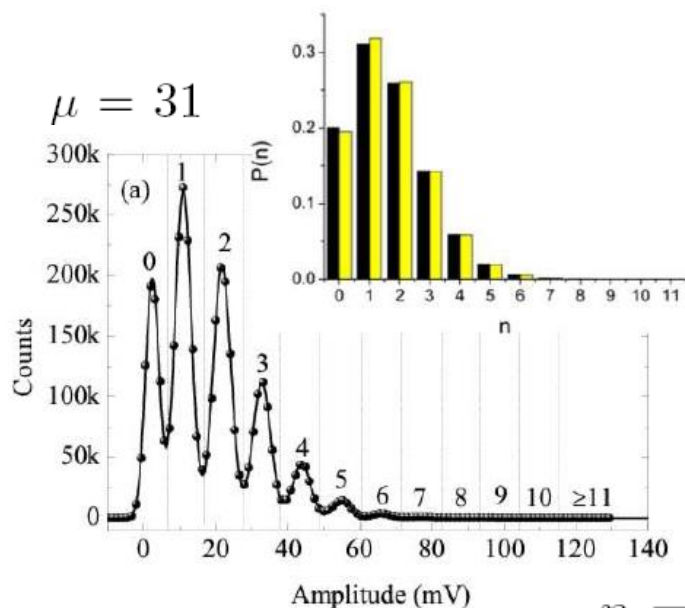
Detector's POVM tomography

Coherent source

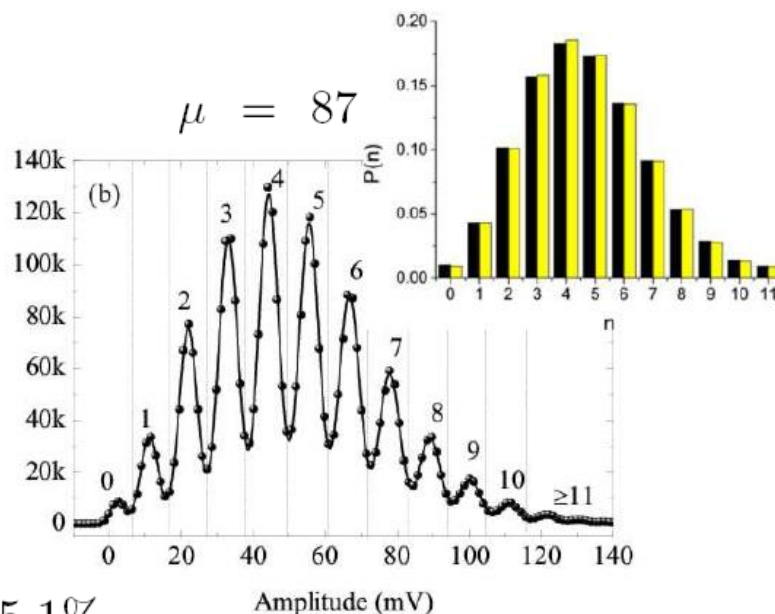
Pulsed laser source



Experiment with a TES



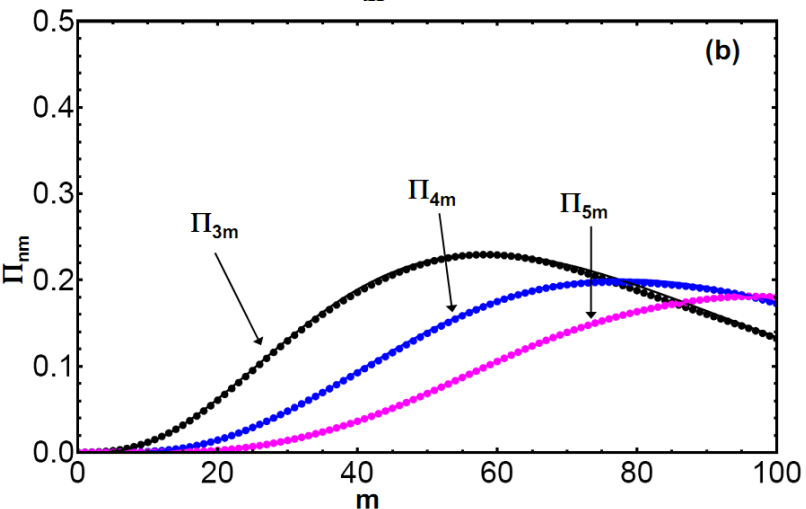
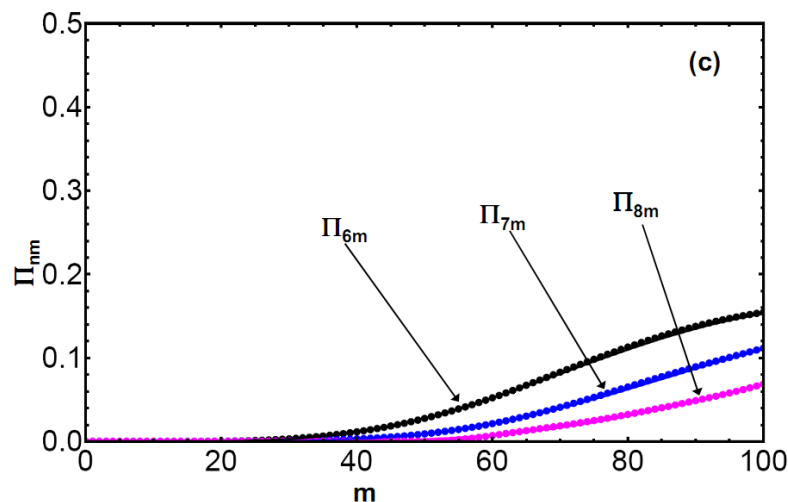
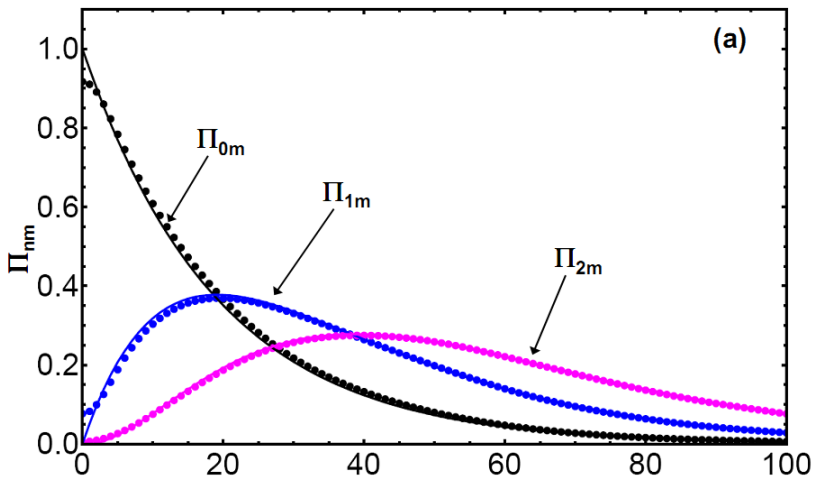
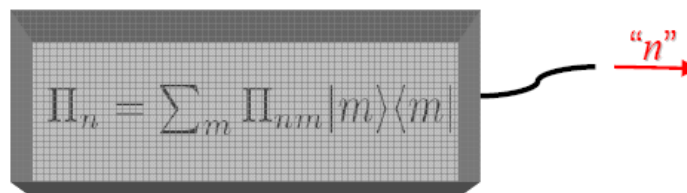
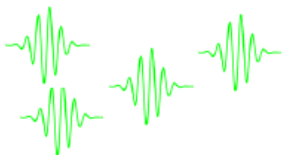
$\eta = 5.1\%$



[NJP 14, 085001 (2012)]

Detector's POVM tomography

Coherent source



Linear detection model

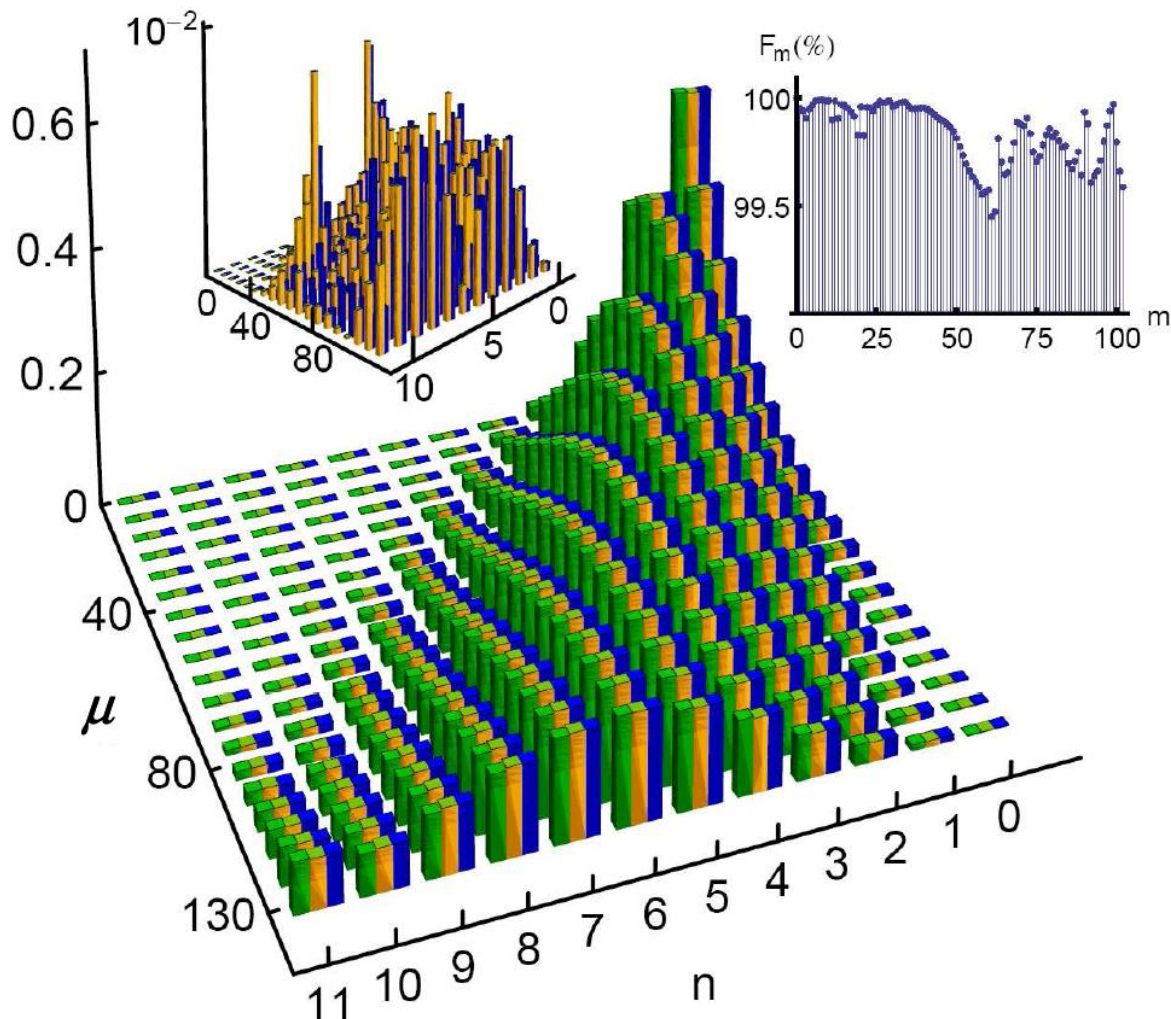
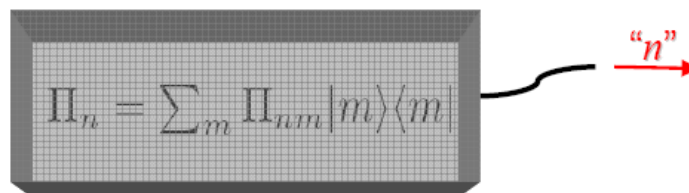
$$\Pi_n = \sum_{m=n}^{\infty} B_{nm} |m\rangle\langle m|$$

$$B_{nm} = \binom{m}{n} \eta^n (1 - \eta)^{m-n}$$

[NJP 14, 085001 (2012)]

Detector's POVM tomography

Coherent source



$$\Pi_n = \sum_{m=n}^{\infty} B_{nm} |m\rangle\langle m|$$

$$B_{nm} = \binom{m}{n} \eta^n (1 - \eta)^{m-n}$$

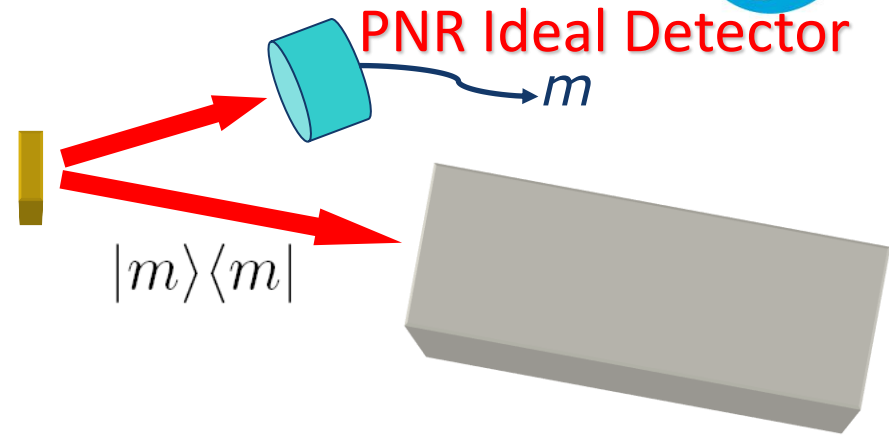
[NJP 14, 085001 (2012)]

Detector's POVM tomography

Simplest Solution:

Heralded Fock state source

$$|R\rangle\rangle = \sum_m R_m |m\rangle|m\rangle$$

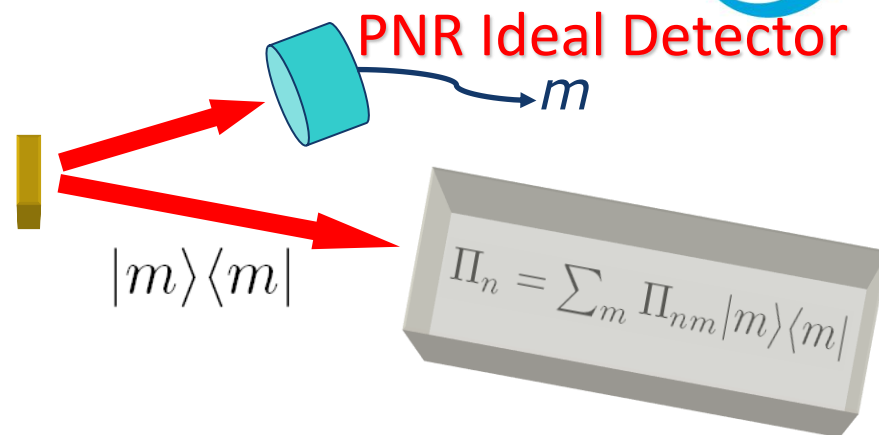


Detector's POVM tomography

Simplest Solution:

Heralded Fock state source

$$|R\rangle\rangle = \sum_m R_m |m\rangle |m\rangle$$

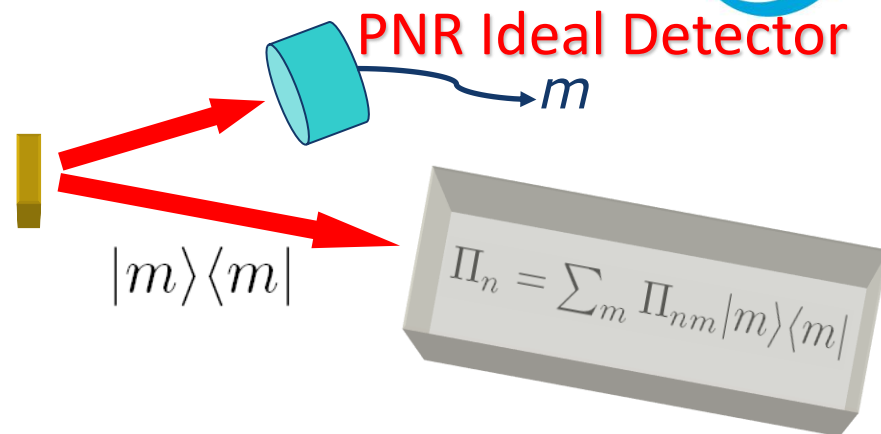


Detector's POVM tomography

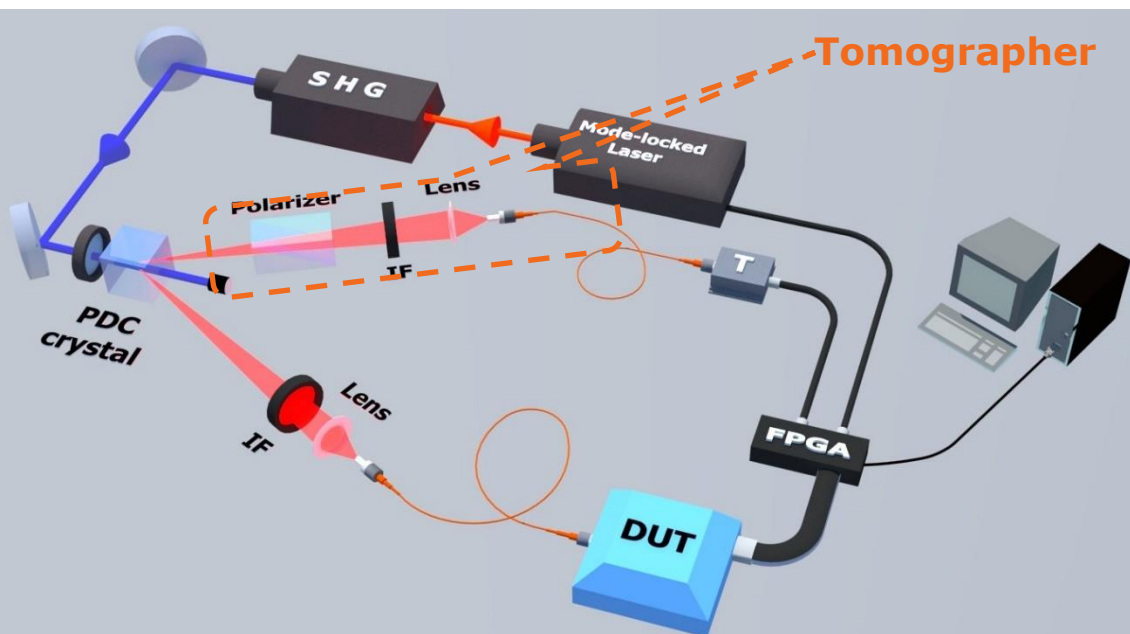
Simplest Solution:

Heralded Fock state source

$$|R\rangle\rangle = \sum_m R_m |m\rangle |m\rangle$$



Affordable Solution: Tomographer on the ancilla arm

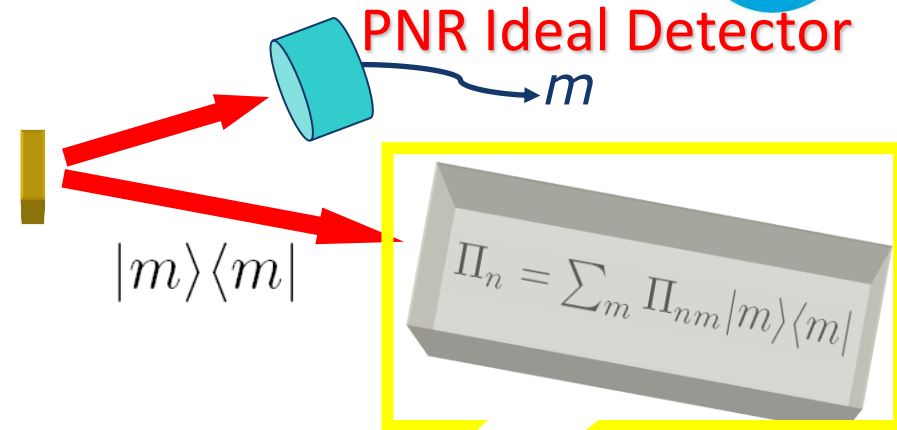


Detector's POVM tomography

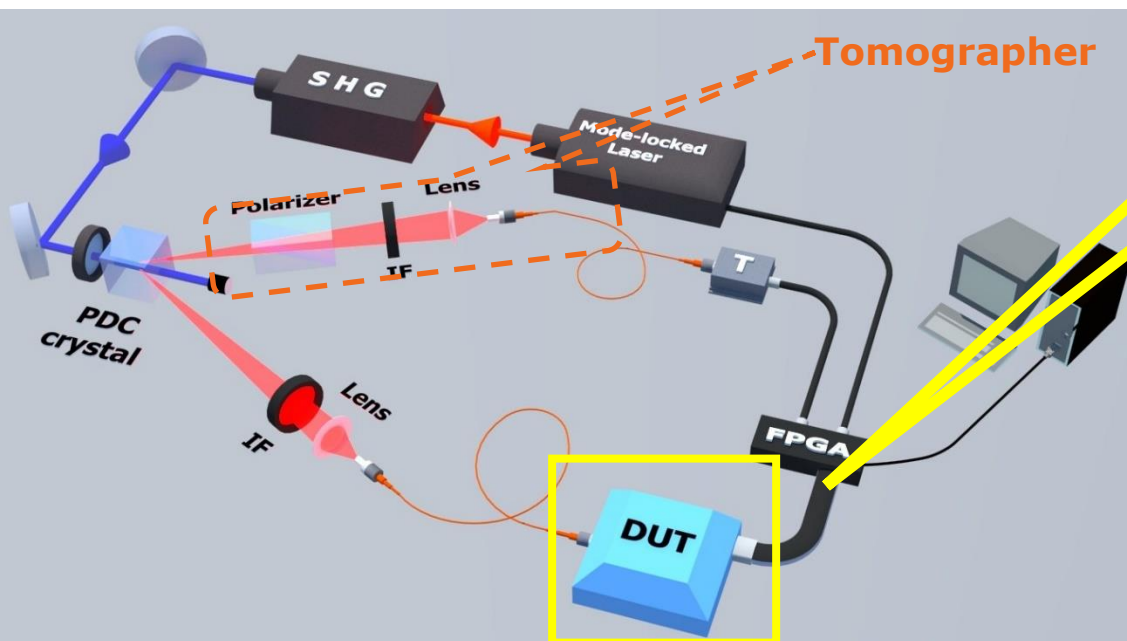
Simplest Solution:

Heralded Fock state source

$$|R\rangle\rangle = \sum_m R_m |m\rangle |m\rangle$$



Affordable Solution: Tomographer on the ancilla arm

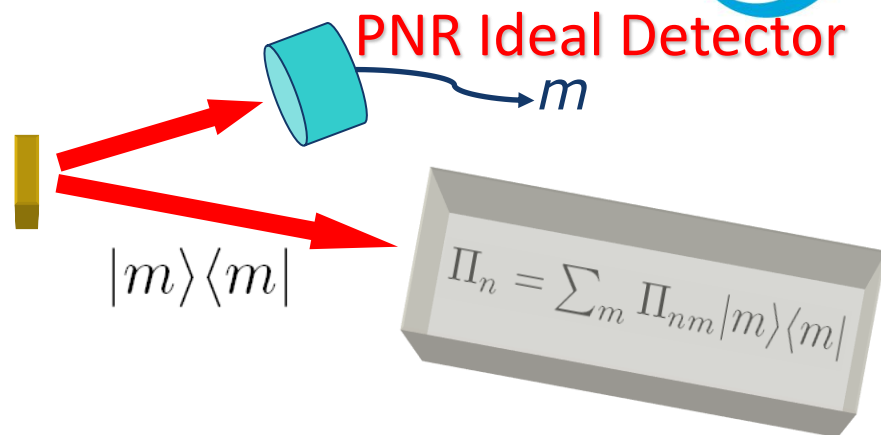


Detector's POVM tomography

Simplest Solution:

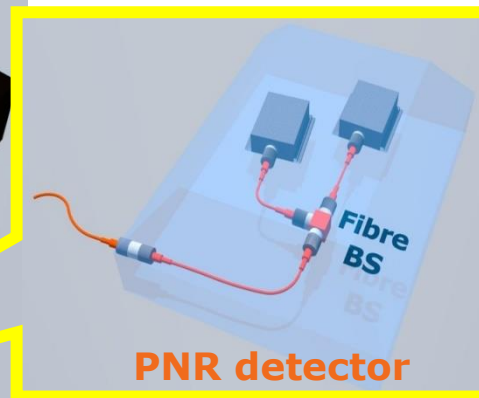
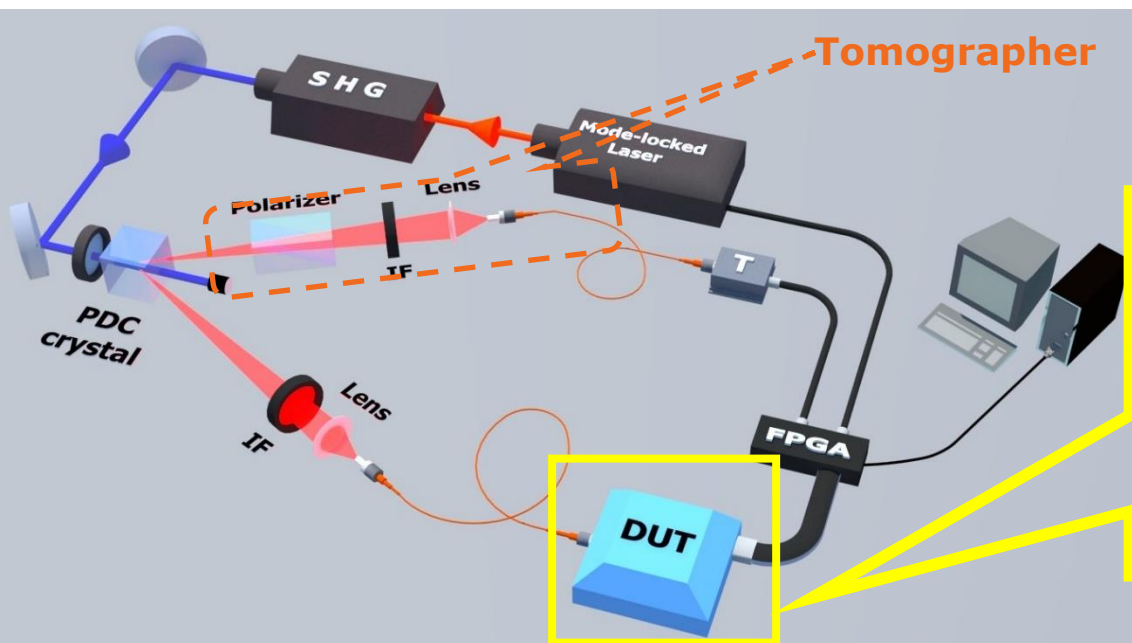
Heralded Fock state source

$$|R\rangle\rangle = \sum_m R_m |m\rangle |m\rangle$$



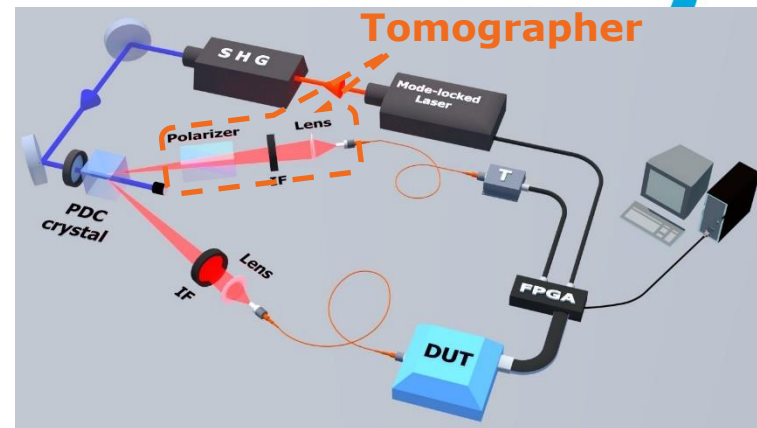
Affordable Solution: Tomographer on the ancilla arm

[PRL **108**, 253601 (2012)]



Detector's POVM tomography

$$|R\rangle\rangle = \sum_m R_m |m\rangle |m\rangle$$

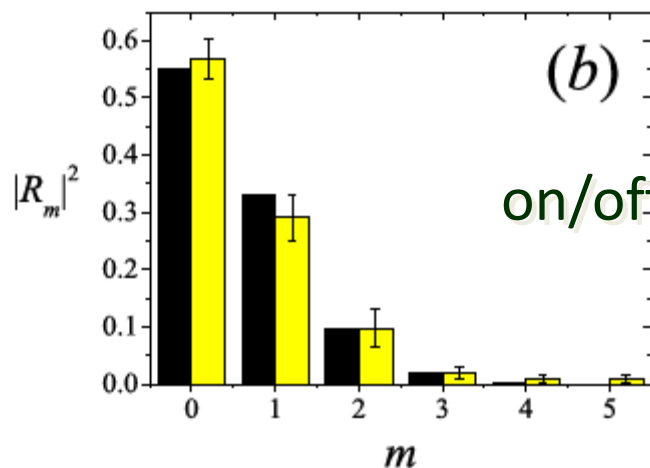
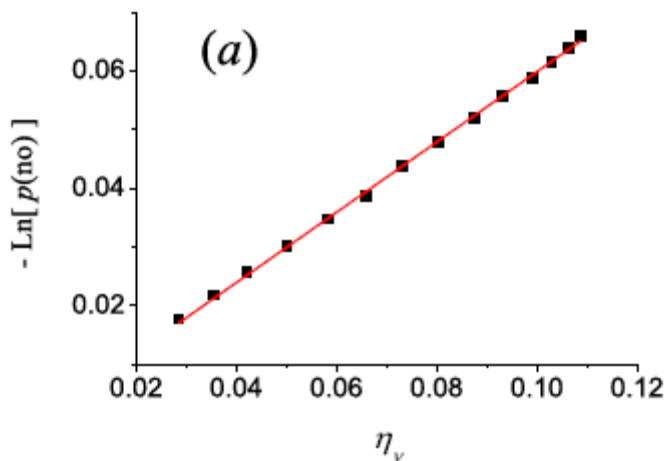


[PRL **108**, 253601 (2012)]

Tomographer on the ancilla arm

$$p(n, \text{yes}) = \sum_m \Pi_{nm} |R_m|^2 [1 - (1 - \eta)^m]$$

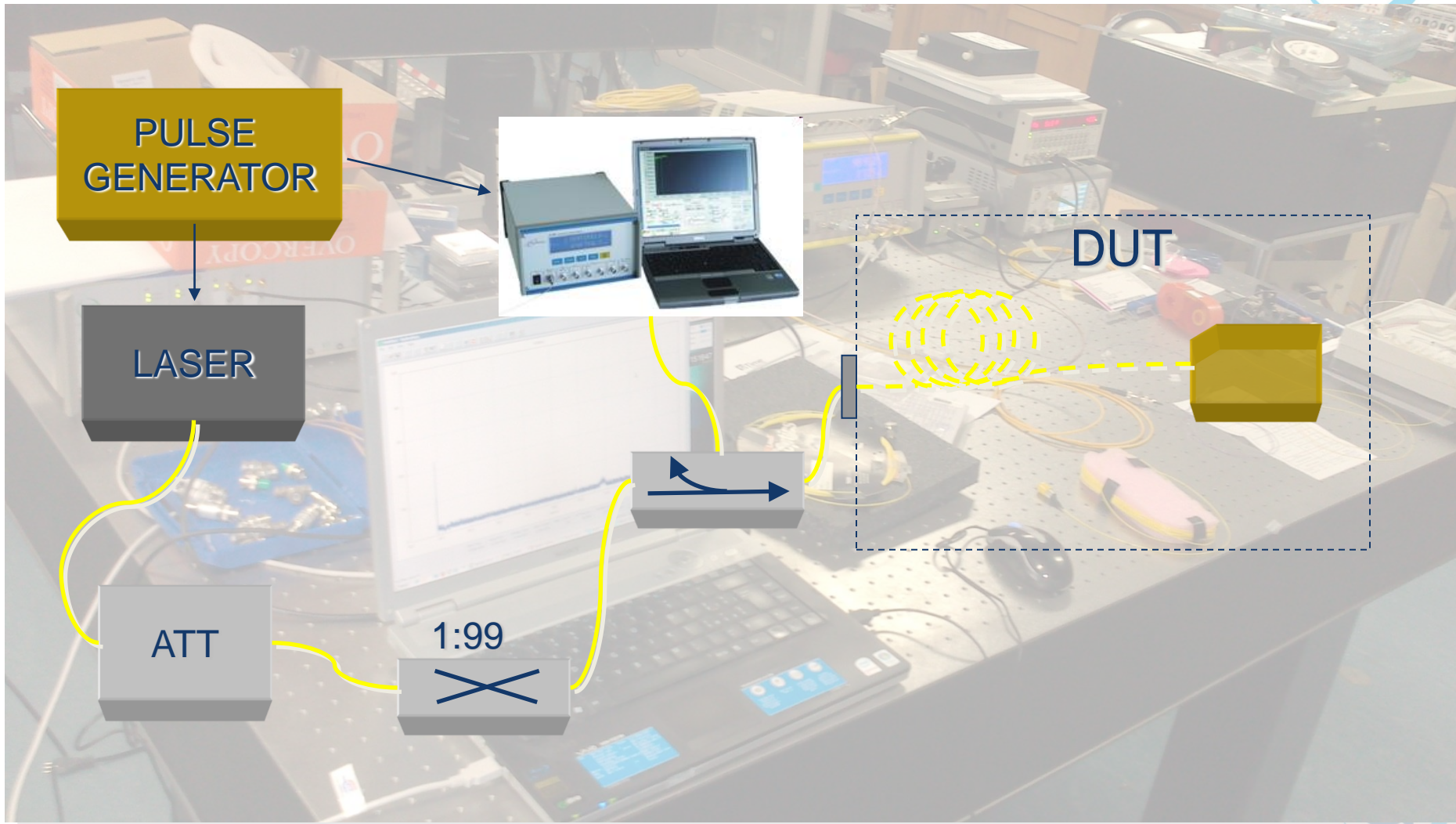
$$p(n, \text{no}) = \sum_m \Pi_{nm} |R_m|^2 (1 - \eta)^m$$



on/off reconstruction

[PRA **70**, 055801 (2004); J. Řeháček et al., PRA **67**, 061801 (2003)]

Detectors' Backflash Emission: a security threat

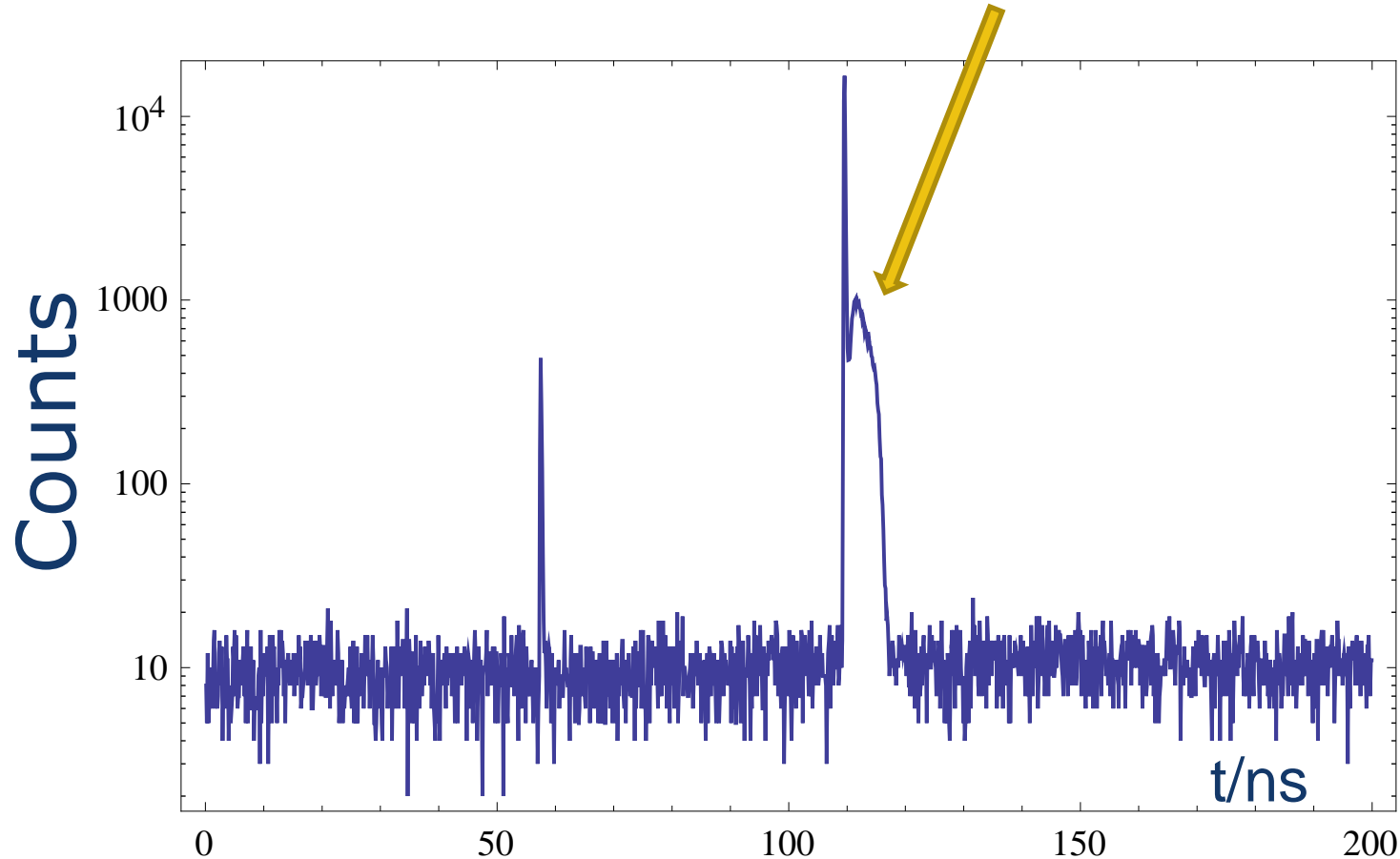


OTDR operating at single-photon level

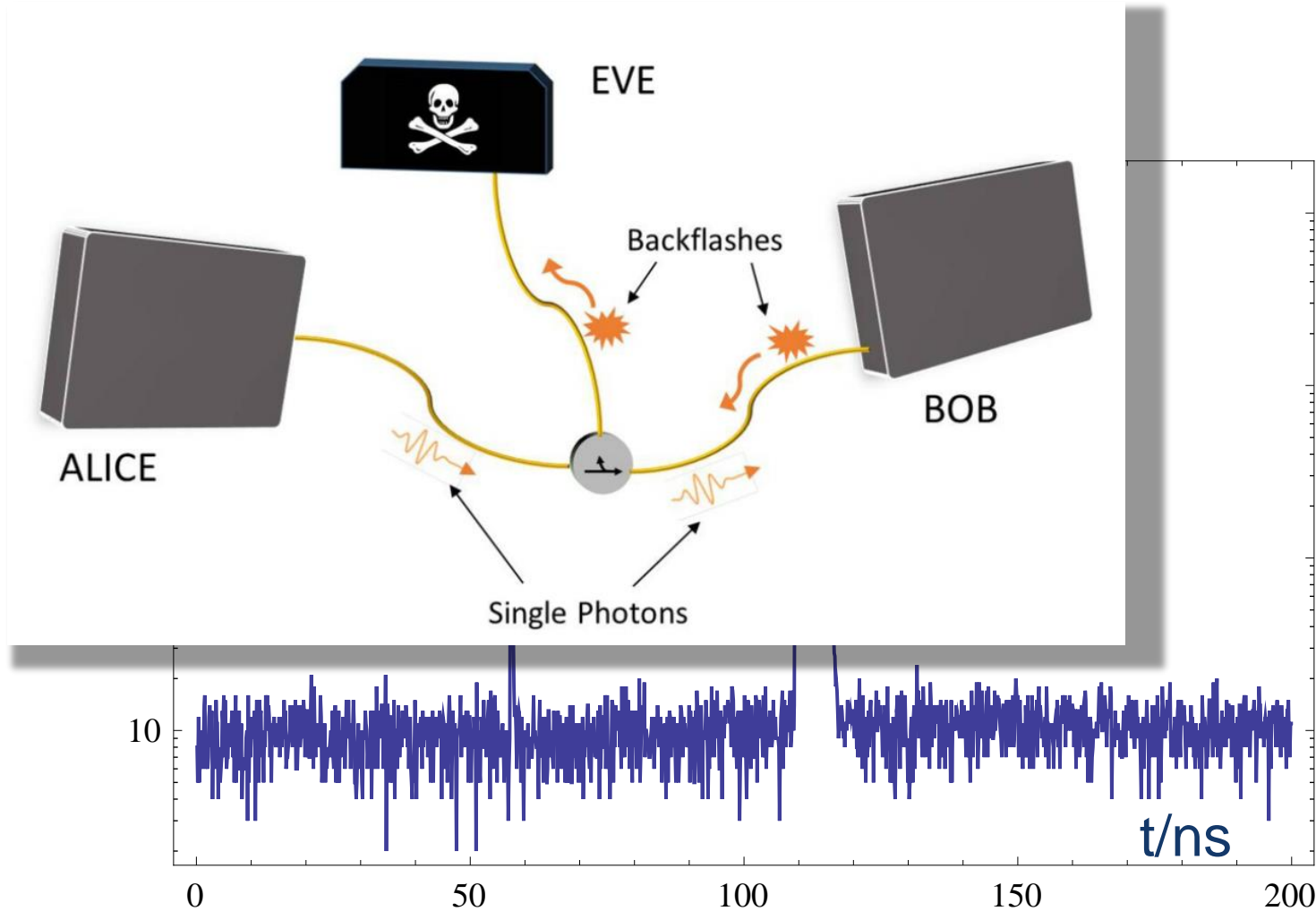
Detectors' Backflash Emission: a security threat



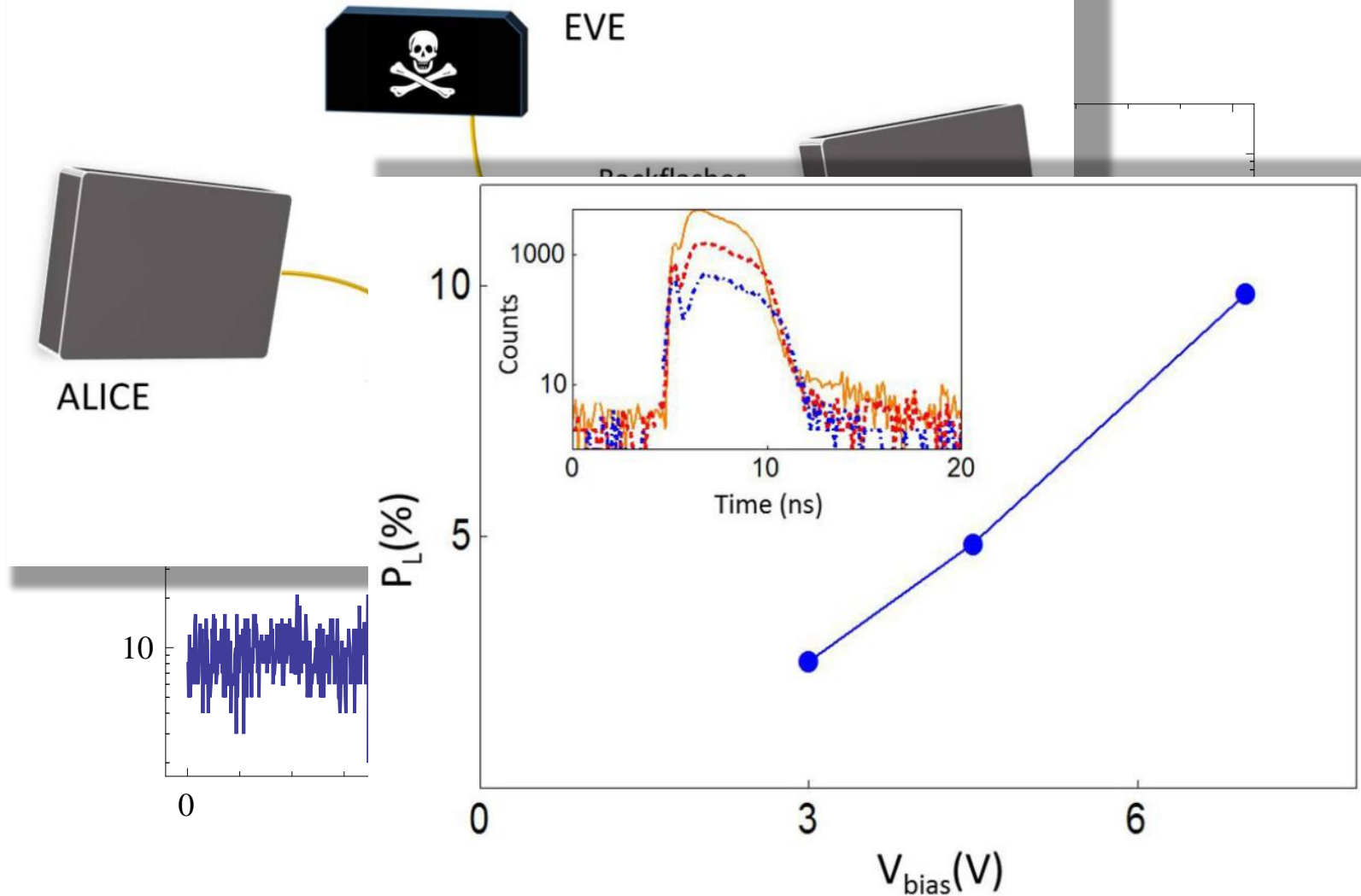
Single-photon-detector Back-Flashes



Detectors' Backflash Emission: a security threat



Detectors' Backflash Emission: a security threat



EURAMET is the Regional Metrology Organisation (RMO) of Europe.

- Cooperation of National Metrology Institutes (NMI) in Europe in research in metrology, traceability of measurements, international recognition of Calibration and Measurement Capabilities (CMC);
- Knowledge Transfer and cooperation among EURAMET members
EURAMET facilitates the development of the metrology infrastructures;
- European Metrology Research Programmes (EMRP and EMPIR) designed to encourage collaboration between European National Metrology Institutes (NMIs) and partners in industry or academia.



European Metrology Networks (EMN) EURAMET



Objective: To create sustainable structures in areas of strategic importance for the future of European metrology.



The Networks...

- cover an area of major strategic importance, with a **European dimension**;
- establish close links with a wider **stakeholder community**; including cooperation with other partnerships;
- strive for **scientific excellence**;
- develop and coordinate a **common metrology strategy & infrastructure** to support innovation, public policy, & regulation.



EMN for Quantum Technologies: EMN-Q



Commitment:

- To become the **unique contact point to stakeholders** interested in metrology for quantum technologies (QT)
- To contribute to **standardisation and certification** of QT
- To promote the **take-up of metrology** in the development of QT
- To promote the use of **quantum measurement techniques** where advantageous for “classical” technical areas
- To support **industrial needs** in synergy with the objectives of the **EC Quantum Flagship** and **national QT programs**



EMN-Q Contact Group



EMN for Quantum Technologies: EMN-Q

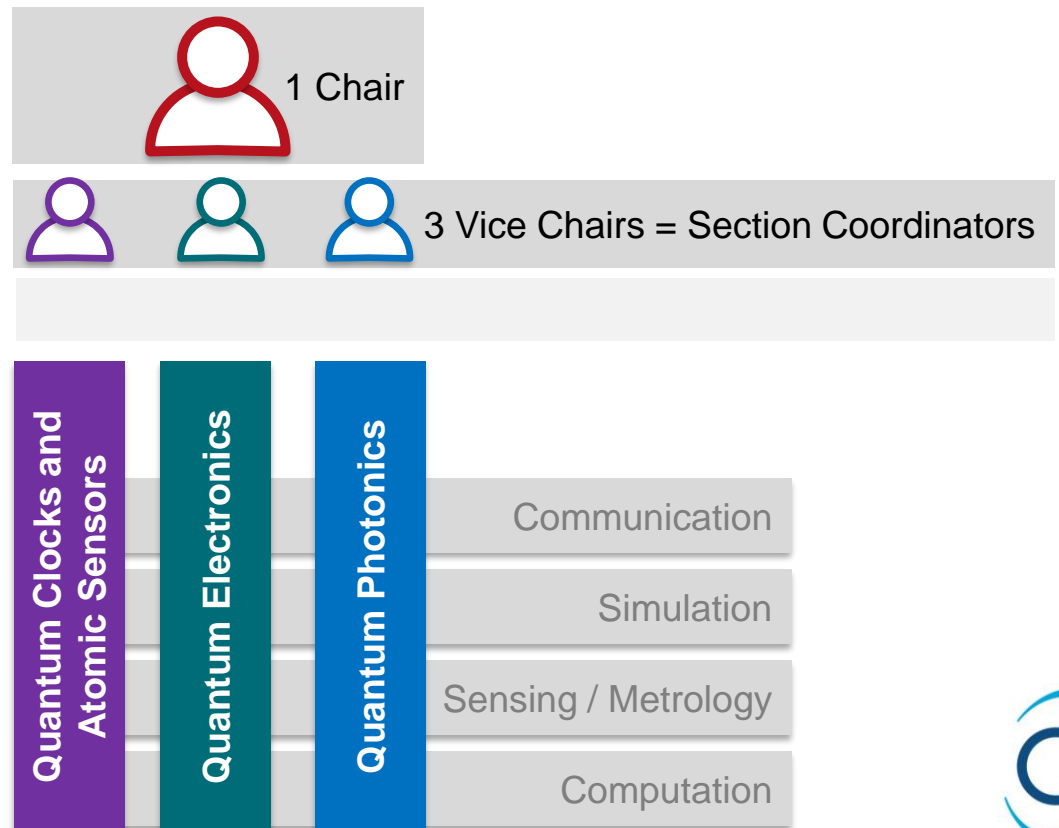
By 20 May 2021,
**18 EURAMET Members
and Partners**
signed the MoU of EMN-Q

Aalto	FI
Metroserit	EE
CEM	SP
CMI	CZ
DFM	DK
GUM	PL
INRIM	IT
IPQ	PT
JV	NO
LNE	FR
LNE-LCM/CNAM	FR
LNE-SYRTE	FR
METAS	CH
VTT-MIKES	FI
NPL	UK
PTB	DE
RISE	SE
UME	TR

EMN-Q: Structure and Organisation



EMN-Q: Structure and Organisation

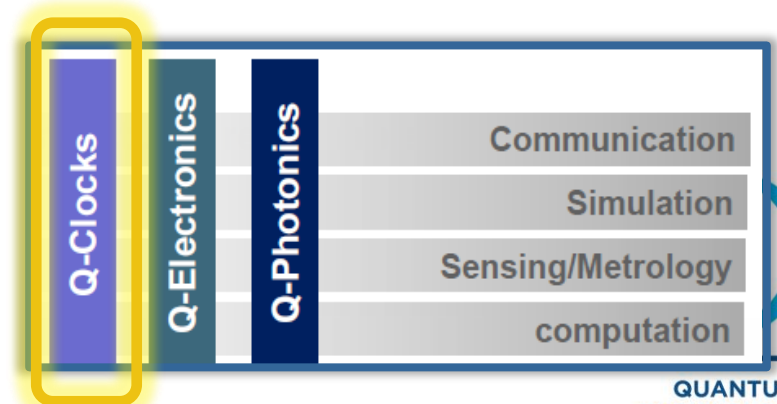


EMN-Q (3 sections)



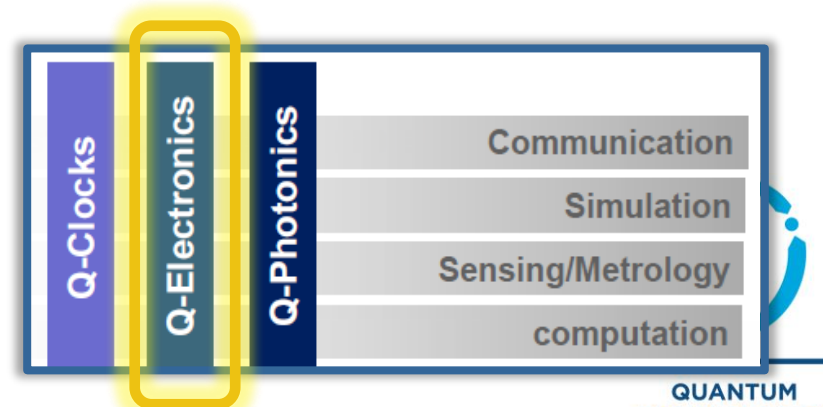
Quantum Clocks and Atomic Sensors

- **New optical clocks** and **quantum-enhanced** techniques (e.g. QND, entanglement-based)
- **EU frequency distribution** fiber network, space network
- **Certified time** and time stamping distribution
- **Atomic sensors:** gravimeters, gyroscopes, ...
- ...



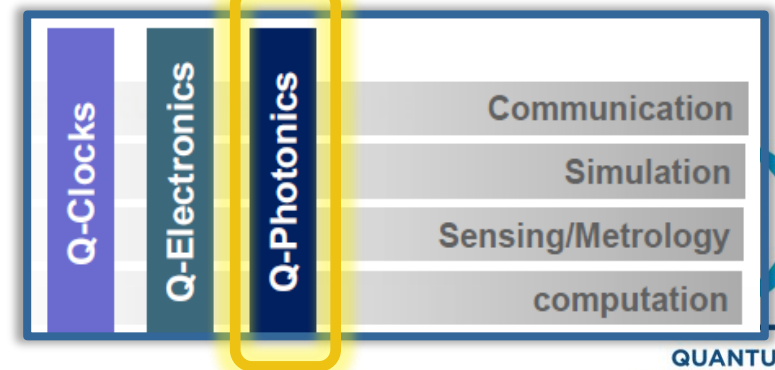
Quantum Electronics

- **Commercial quantum electrical standards** with graphene
- **Topological insulators**
- **Novel quantum devices** based on, e.g., superconducting nanostructures or semiconducting quantum dots for **electrical metrology and sensing**
- ...



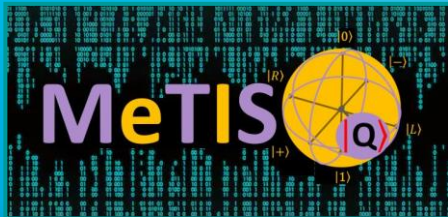
Quantum Photonics

- Traceability of measurement at **single photon level**
- **Metrology for QKD** in fiber and QKD testbeds, metrology for QKD in space
- **Quantum imaging**: metrology but also R&D
- **Quantum** (magnetic, pressure, temperature) **sensors** based on colour centers
- ...





QUANTUM TECHNOLOGIES

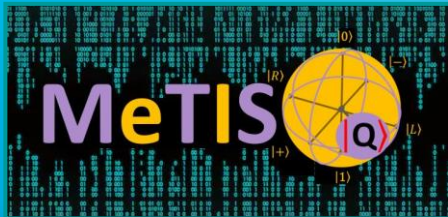


19NET02 «EMN-Quantum»
EMPIR  

The EMPIR initiative is co-funded by the European Union's Horizon 2020 research and innovation programme and the EMPIR Participating States

Thanks for your
attention!

QUANTUM
TECHNOLOGIES



19NET02 «EMN-Quantum»

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